

## Supplementary Materials

### Machine learning-driven optimization of plasma-coupled photocatalytic CO<sub>2</sub> reduction system for syngas production

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### Experimental equipment and processes

The plasma-photocatalytic CO<sub>2</sub> reduction (P<sup>2</sup>CR) experiments were carried out in a custom-built dielectric barrier discharge (DBD) reactor system (Beijing Perfectlight Technology Co., Ltd.), as shown in Supplementary Figure 1. The setup consisted of a square quartz reactor (100×100×50 mm, wall thickness 3 mm), a high-voltage power supply, a 300 W Xe lamp, mass flow controllers (Brooks Instrument, GF40 series), a humidification module, and an online gas-analysis system. The reactor was operated at atmospheric pressure using high-purity CO<sub>2</sub> as the feed gas and Ar as carrier gas, with the CO<sub>2</sub>/Ar volume ratio maintained at 1:1 using the mass flow controllers. The total inlet gas flow rate (CO<sub>2</sub>+Ar) was varied from 20 to 60 mL min<sup>-1</sup>, corresponding to a nominal gas residence time of 20–60 s based on the effective discharge volume (about 20 cm<sup>3</sup>) defined by the electrode area and the 2 mm discharge gap. The relative humidity was controlled in the range of 32–58%. Before each experiment, stable gas-flow and humidity conditions were established using a temperature-controlled humidification system, and the relative humidity was continuously monitored using a hygrometer (OHR-WS50R-S3-D1-G1-01-A). During operation, the reactor was connected to an external circulating water-cooling system maintained at 30 °C to reduce bulk temperature fluctuations. The outer surface temperature of the reactor was monitored using an infrared thermal imaging camera (Testo 868) to qualitatively assess the thermal effect induced by plasma discharge and light irradiation. In the reaction zone, certain amount of photocatalyst was uniformly distributed over the bottom-electrode region of the reactor. DBD plasma was generated with a fixed electrode gap of 2 mm, while continuous irradiation from a 300 W Xe lamp (PLS-SXE300D/300DUV, Beijing Perfectlight) was introduced vertically from the top of the reactor without an optical filter, with a lamp-to-catalyst distance of 10 cm. The nominal incident light intensity was varied from 600 to 1400 mW cm<sup>-2</sup>. The electrical characteristics of the discharge were recorded using a Tektronix TBS2000 oscilloscope equipped with a high-voltage probe (Tektronix P5200A) and a high-frequency current probe (Tektronix CT1F). The plasma was operated at a fixed

frequency of 10 kHz, and the discharge condition was adjusted by varying the applied voltage from 10 to 50 V. Before catalytic testing, each gas chromatographic (GC) system was calibrated independently using certified standard gas mixtures within its own validated linear response range. For the plasma-catalytic and plasma-photocatalytic experiments, where the gaseous product concentrations were relatively high, gas products were analysed using a conventional GC system (GC-8090PLUS) equipped with thermal conductivity detector (TCD) and flame ionization detector (FID) modules (100 ppm detection threshold). The quantification of H<sub>2</sub>, CO, and CO<sub>2</sub> was based on the TCD response, whereas the FID channel was used only to screen for possible hydrocarbons and oxygenated organic byproducts. For the light-only photocatalytic experiments, because the CO concentration was substantially lower than that observed under plasma-only and plasma-photocatalytic conditions, trace CO was quantified using a dedicated high-sensitivity GC system (GC-7090II). In this system, CO was first catalytically converted and then detected by FID, enabling reliable trace-CO analysis in the low-concentration regime (1 ppm detection threshold). A separate calibration curve for trace CO was established for this analytical channel using certified standard gas mixtures in the corresponding low-concentration range. Product concentrations were obtained by converting detector peak areas using the corresponding calibration curves of each instrument. For each catalyst, control experiments were conducted using the same catalyst loading and feed-gas composition. All experiments were independently repeated three times.

To evaluate the performance of the photocatalyst, the yield of the products and the conversion rate of the reactants are calculated by using the following formulas.

The conversion of CO<sub>2</sub>:<sup>[1]</sup>

$$X_{CO_2}(\%) = \frac{CO_2 \text{ input} - CO_2 \text{ output}}{CO_2 \text{ input}} \times 100 \quad (1)$$

The yield of product gas:<sup>[2]</sup>

$$Yield_{CO\ or\ H_2}(mmol\ g^{-1}\ h^{-1}) = \frac{n_{CO\ or\ H_2}}{Weight\ of\ catalyst} \times 60 \quad (2)$$

where,  $n_{CO\ or\ H_2} = \frac{F \times V}{22.4}$ , F is gas flow rate (mL min<sup>-1</sup>). V is the measured concentration of the product gas (vol.%). In Eq. (2), V is divided by 100 to convert vol.% to a dimensionless volume fraction.

### Photocatalyst preparation

Cu–Pd/TiO<sub>2</sub> photocatalysts were synthesized via a conventional wet impregnation method. The total metal loading was fixed at 5 wt% relative to TiO<sub>2</sub>. In a typical procedure, 1.0 g of TiO<sub>2</sub> powder was dispersed in deionized water and ultrasonicated to obtain a homogeneous suspension. Aqueous solutions of copper nitrate trihydrate and palladium nitrate were separately prepared to achieve a Cu:Pd metal molar ratio of 1:1, followed by ultrasonic treatment and subsequent mixing to form a uniform metal precursor solution. The prepared precursor solution was then introduced dropwise into the TiO<sub>2</sub> suspension under continuous ultrasonication to ensure uniform dispersion of metal species on the support. The resulting mixture was further stirred and aged at room temperature to facilitate sufficient metal precursor adsorption onto the TiO<sub>2</sub> surface. Subsequently, the sample was dried under vacuum at 100 °C to remove residual solvent and finally calcined in air at 500 °C to obtain the Cu–Pd/TiO<sub>2</sub> photocatalyst.

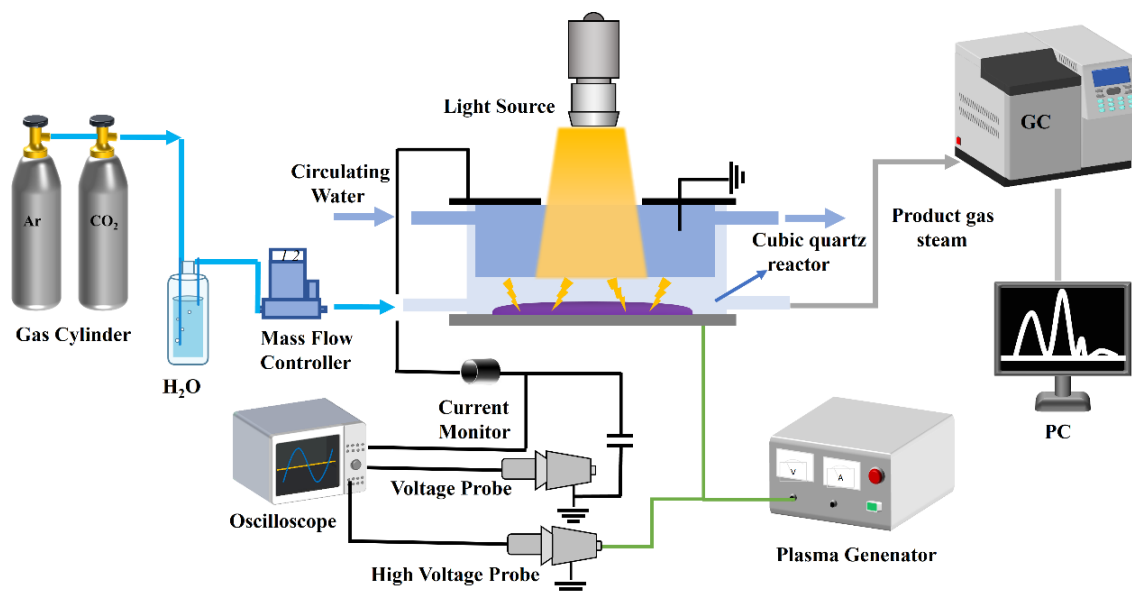
### Low–High Pairwise Interaction Screening

A low–high 2×2 model-based screening was performed to evaluate the conditional dependence between pairs of operating variables. For each variable pair, the two selected variables were set to their experimentally observed lower and upper levels, while the remaining variables were fixed at representative central conditions: discharge power of 50 W, catalyst dosage of 40 mg, gas flow rate of 40 mL min<sup>-1</sup>,

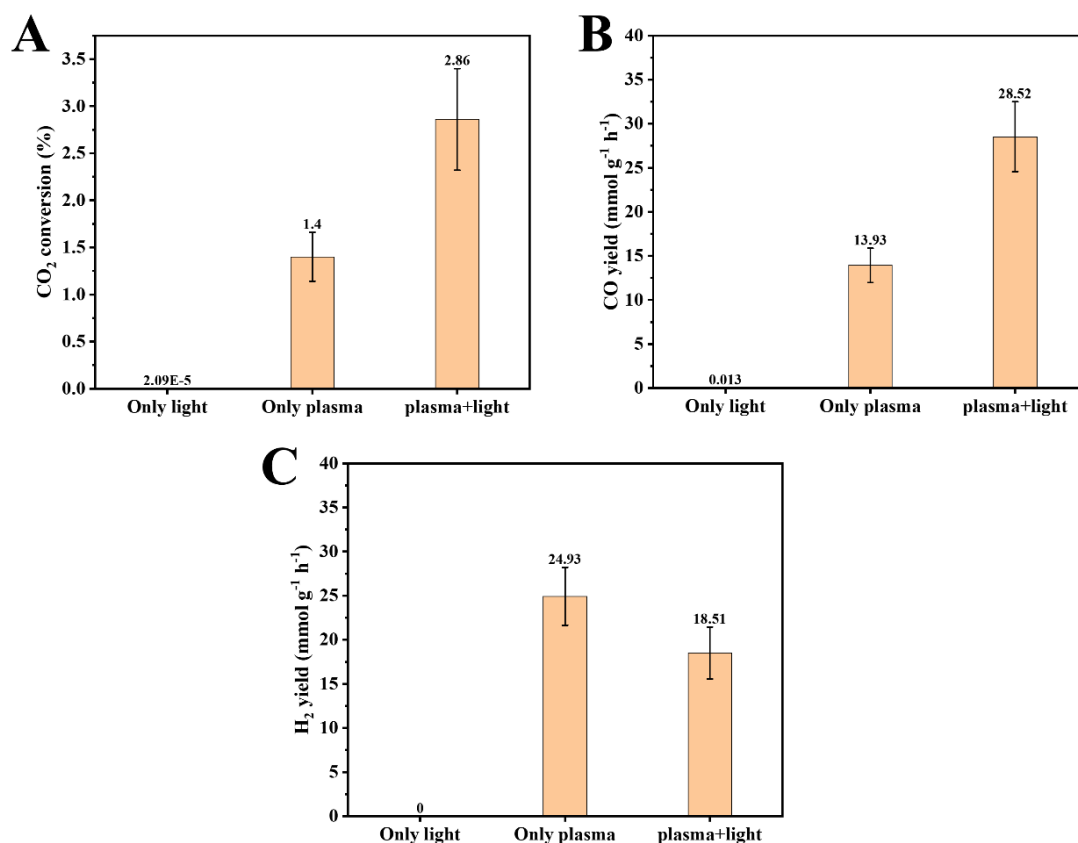
relative humidity of 40%, and light intensity of  $1000 \text{ mW cm}^{-2}$ . The conditional interaction contrast was calculated as follows:

$$\text{Interaction contrast} = Y_{\text{high,high}} - Y_{\text{low,high}} - Y_{\text{high,low}} - Y_{\text{low,low}} \quad (3)$$

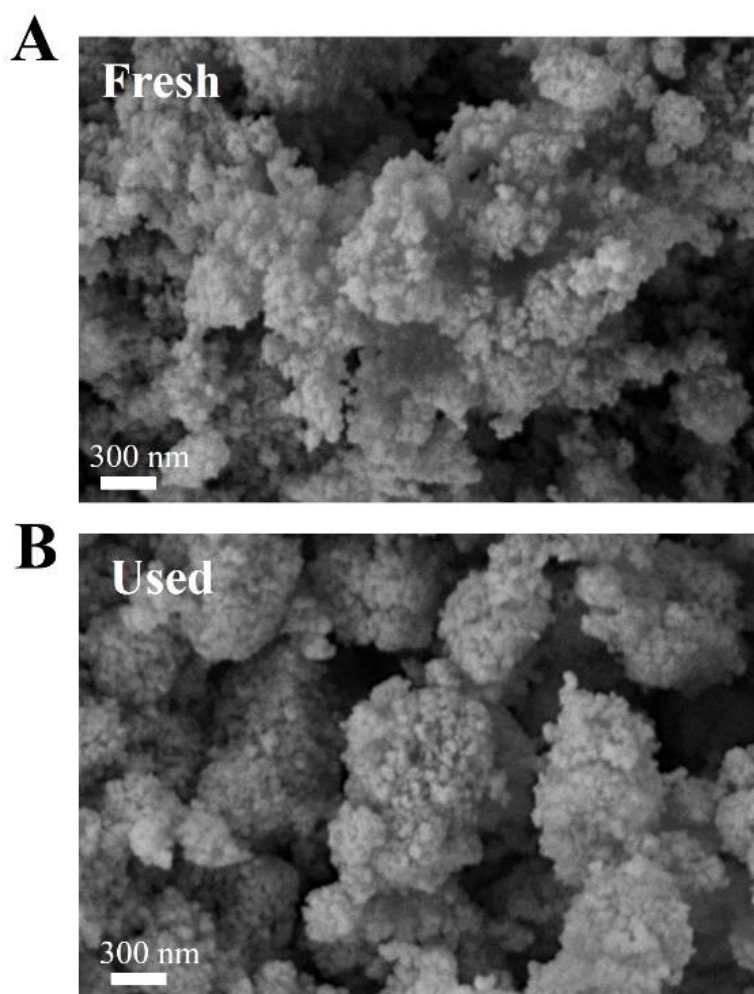
where Y represents the model-predicted output. A positive value indicates that the combined high-level condition produces a response higher than the additive expectation, whereas a negative value indicates a response lower than the additive expectation. This screening is exploratory and represents model-predicted conditional relationships rather than a factorial experiment or direct evidence of reaction mechanisms.



**Supplementary Figure 1.** Scheme of P<sup>2</sup>CR system.

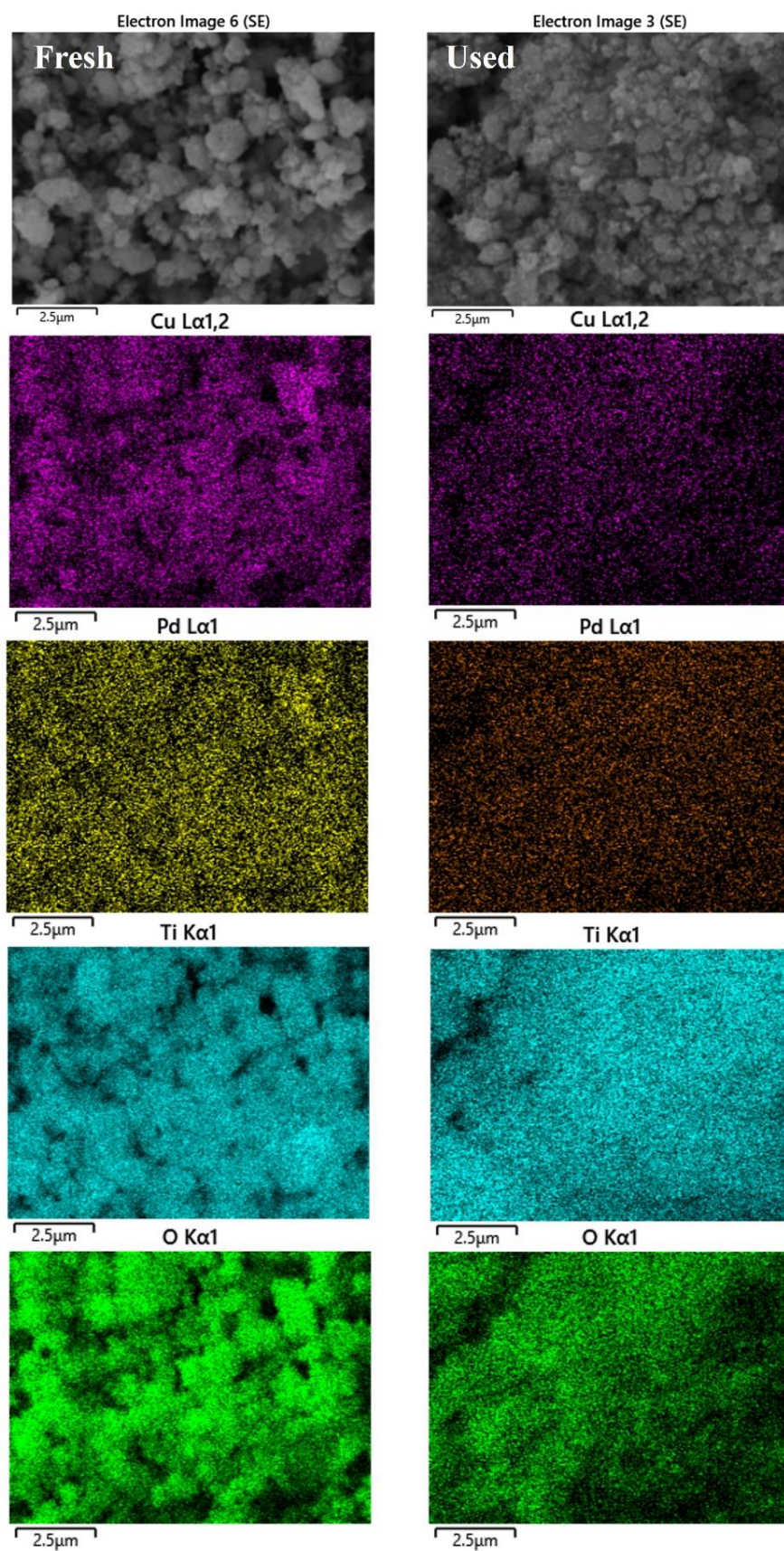


**Supplementary Figure 2.** Catalytic performance of (A) CO<sub>2</sub> conversion, (B) CO yield and (C) H<sub>2</sub> yield of Cu–Pd/TiO<sub>2</sub> under only-light, only-plasma and plasma–light coupling conditions, respectively. (Discharge power: 60 W, catalysts dose: 30 mg, gas flow: 30 mL min<sup>-1</sup>, relative humidity 50%, light intensity: 1000 mW cm<sup>-2</sup>).



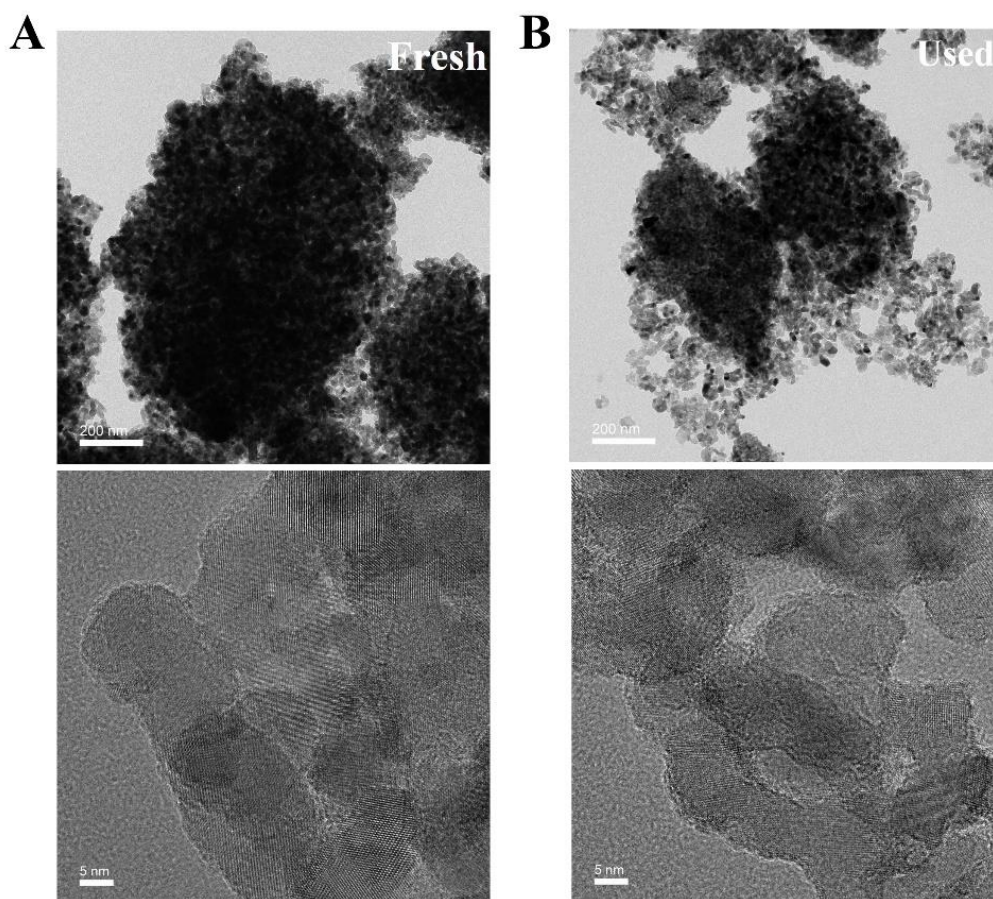
**Supplementary Figure 3.** SEM images of (A) fresh and (B) used Cu–Pd/TiO<sub>2</sub>.

SEM images of fresh and used Cu–Pd/TiO<sub>2</sub> catalysts are shown in Supplementary Figure 3. After catalytic reaction, the used catalyst maintains a similar particle aggregation structure without obvious collapse or severe sintering, suggesting good structural stability during the photocatalytic process.



**Supplementary Figure 4.** The EDS mapping of fresh and used Cu–Pd/TiO<sub>2</sub> photocatalyst.

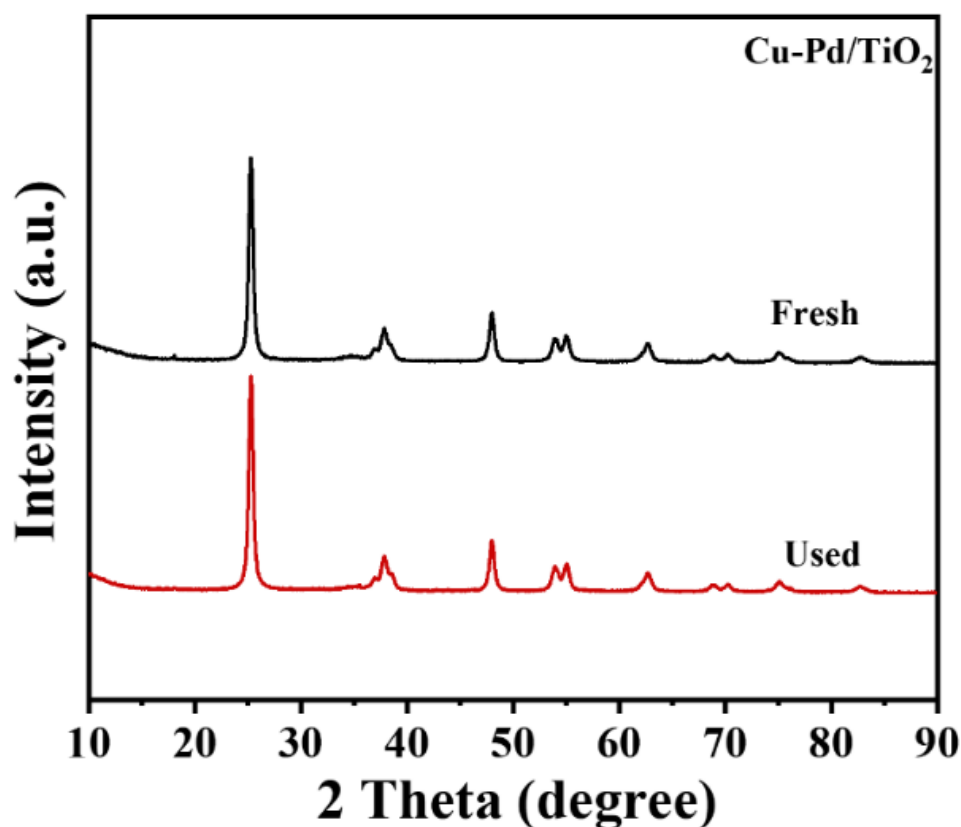
The elemental mapping results demonstrate the homogeneous distribution of Cu, Pd, Ti, and O elements throughout both fresh and used Cu–Pd/TiO<sub>2</sub> catalysts. The uniform dispersion of Cu and Pd species indicates that the noble metal and transition metal components are successfully anchored onto the TiO<sub>2</sub> support rather than forming largely isolated aggregates. After reaction, the elemental distributions remain almost unchanged, confirming that Cu and Pd species are not significantly leached during the catalytic process. The preserved elemental dispersion contributes to the excellent catalytic durability of the Cu–Pd/TiO<sub>2</sub> catalyst.



**Supplementary Figure 5.** The HR-TEM images of (A) fresh and (B) used Cu–Pd/TiO<sub>2</sub> photocatalyst.

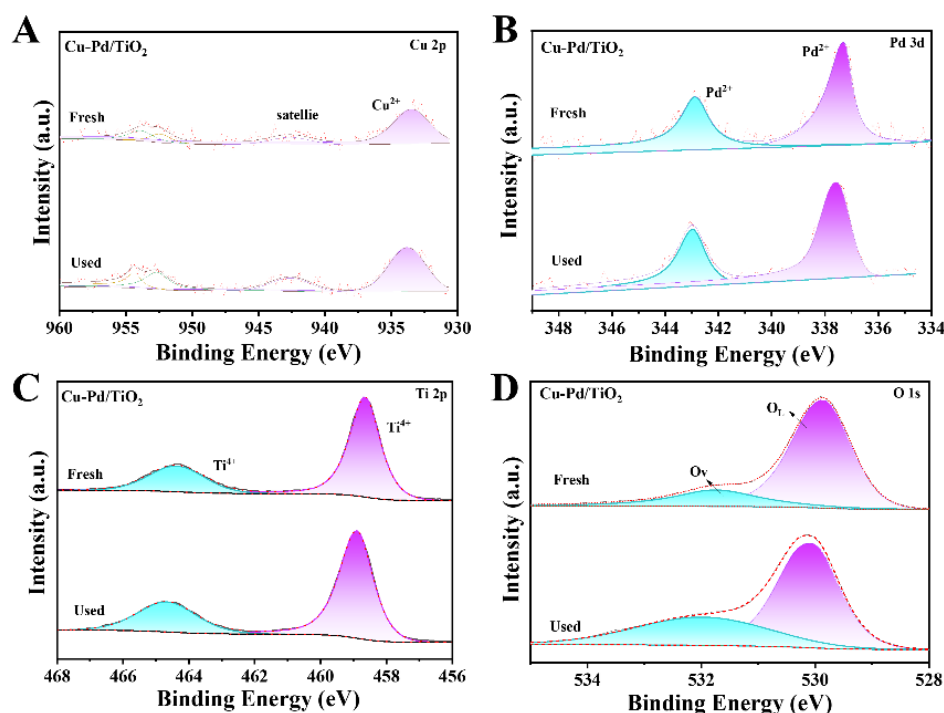
The HR-TEM images reveal that both fresh and used Cu–Pd/TiO<sub>2</sub> catalysts consist of nanosized particles uniformly dispersed on the TiO<sub>2</sub> matrix. After catalytic reaction,

the used catalyst preserves the nanoscale morphology without obvious particle growth or aggregation. The absence of significant structural degradation further confirms the high stability of Cu–Pd/TiO<sub>2</sub> during reaction.



**Supplementary Figure 6.** XRD patterns of fresh and used Cu–Pd/TiO<sub>2</sub> photocatalyst.

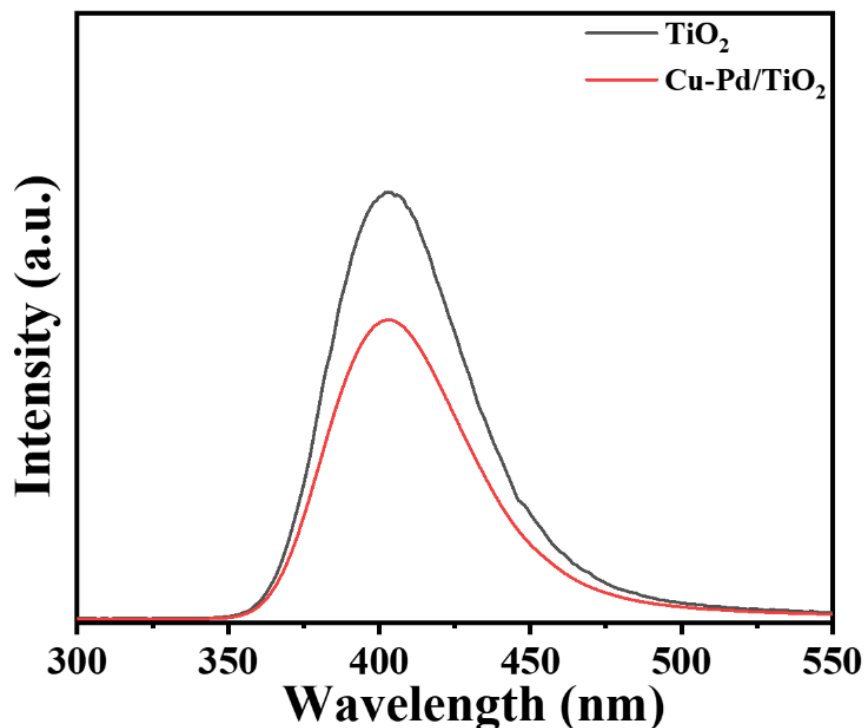
The XRD patterns of fresh and used Cu–Pd/TiO<sub>2</sub> catalysts are presented in Supplementary Figure 6. Both samples show characteristic diffraction peaks assigned to the anatase TiO<sub>2</sub> phase, indicating that TiO<sub>2</sub> remains as the dominant crystalline structure. No obvious diffraction peaks corresponding to Cu or Pd species are detected, which may be attributed to their low loading amount, high dispersion, or small particle size. After reaction, the diffraction pattern of the used catalyst remains almost unchanged, suggesting that the crystalline structure of the catalyst is well preserved during photocatalysis.



**Supplementary Figure 7.** XPS spectra of (A) Cu 2p, (B) Pd 3d, (C) Ti 2p and (D) O 1s of fresh and used Cu-Pd/TiO<sub>2</sub> photocatalyst.

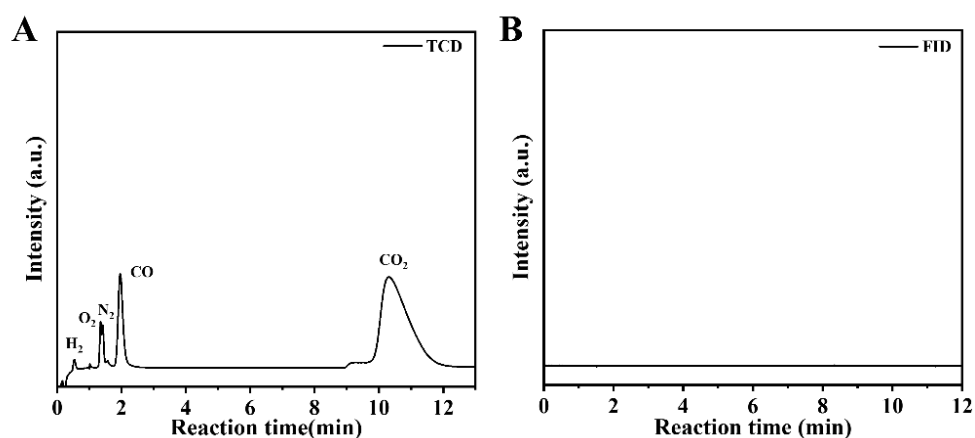
The Cu 2p XPS spectra in Supplementary Figure 7A show characteristic Cu species on the Cu-Pd/TiO<sub>2</sub> catalyst. The Cu 2p<sub>3/2</sub> peak located around 933–935 eV can be attributed to Cu<sup>2+</sup> species. After reaction, the preservation of Cu signals indicates that Cu species remain anchored on TiO<sub>2</sub> without significant loss. The Pd 3d spectra in Supplementary Figure 7B display two characteristic peaks corresponding to Pd 3d<sub>5/2</sub> and Pd 3d<sub>3/2</sub>. The peaks can be assigned to oxidized Pd<sup>2+</sup> species. After catalytic reaction, the Pd signals remain detectable with only minor variations, indicating that Pd species possess good stability. The Ti 2p spectra in Supplementary Figure 7C exhibit two typical peaks corresponding to Ti 2p<sub>3/2</sub> and Ti 2p<sub>1/2</sub>, which are assigned to Ti<sup>4+</sup> species in TiO<sub>2</sub>. No obvious change is observed after reaction, suggesting that the TiO<sub>2</sub> framework remains stable. The maintained Ti<sup>4+</sup> state indicates that the support structure is not significantly reduced or damaged during reaction. The O 1s spectra in Supplementary Figure 7D can be deconvoluted into lattice oxygen species and oxygen

vacancies. Compared with the fresh catalyst, the used sample shows variation in the relative contribution of oxygen vacancies.



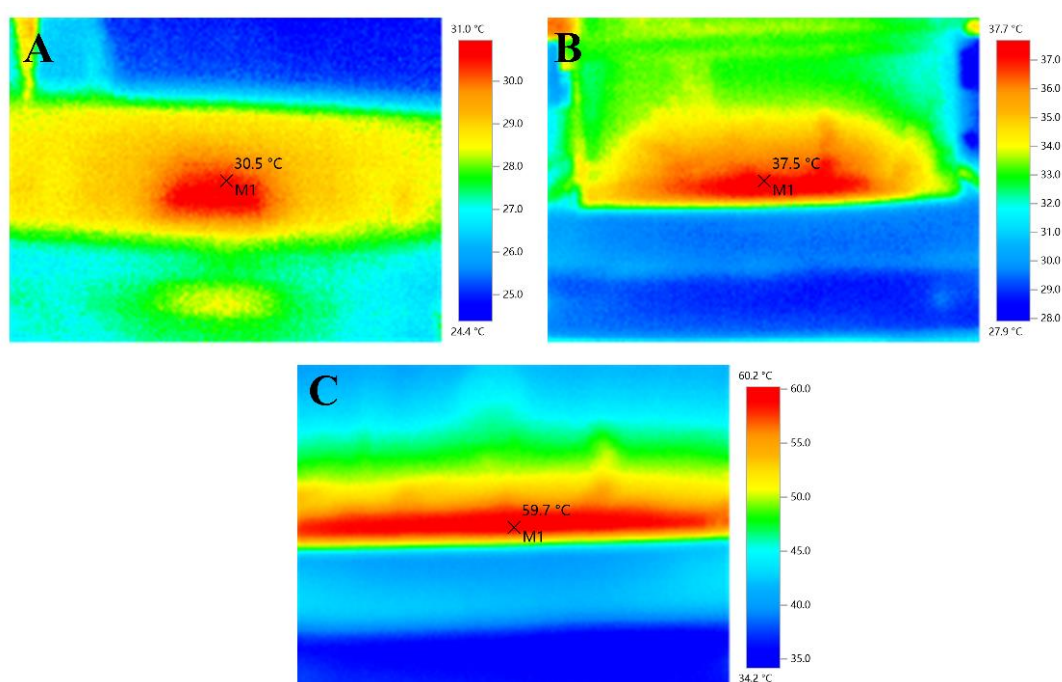
**Supplementary Figure 8.** PL spectra of  $\text{TiO}_2$  and  $\text{Cu-Pd/TiO}_2$  photocatalyst.

The PL spectra in Supplementary Figure 8 indicates that  $\text{Cu-Pd/TiO}_2$  exhibits the highest charge separation efficiency compared with  $\text{TiO}_2$ .

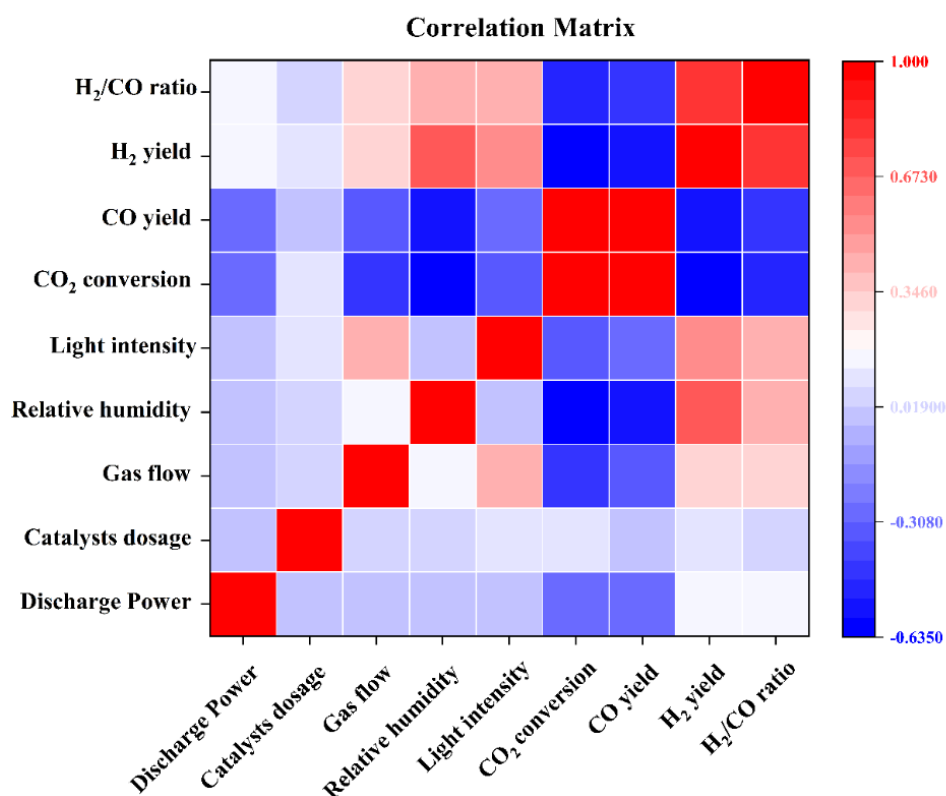


**Supplementary Figure 9.** (A) TCD chromatogram of  $\text{H}_2$  and  $\text{CO}$  and (B) FID chromatogram of hydrocarbon products generated from reduction of  $\text{CO}_2$  and  $\text{H}_2\text{O}$  catalysed by the collaboration of  $\text{Cu-Pd/TiO}_2$  catalyst, DBD plasma and light.

To investigate the formation of possible carbon-containing products, the reactor effluent was simultaneously analysed using both TCD and FID detectors. As shown in Supplementary Figure 9, no detectable peaks corresponding to methane, methanol, ethanol, ethane, or other hydrocarbons or oxygenated compounds were observed in the FID chromatograms within the detection limit of the GC system. Therefore, under the present experimental conditions, CO was identified as the only detectable carbon-containing product.



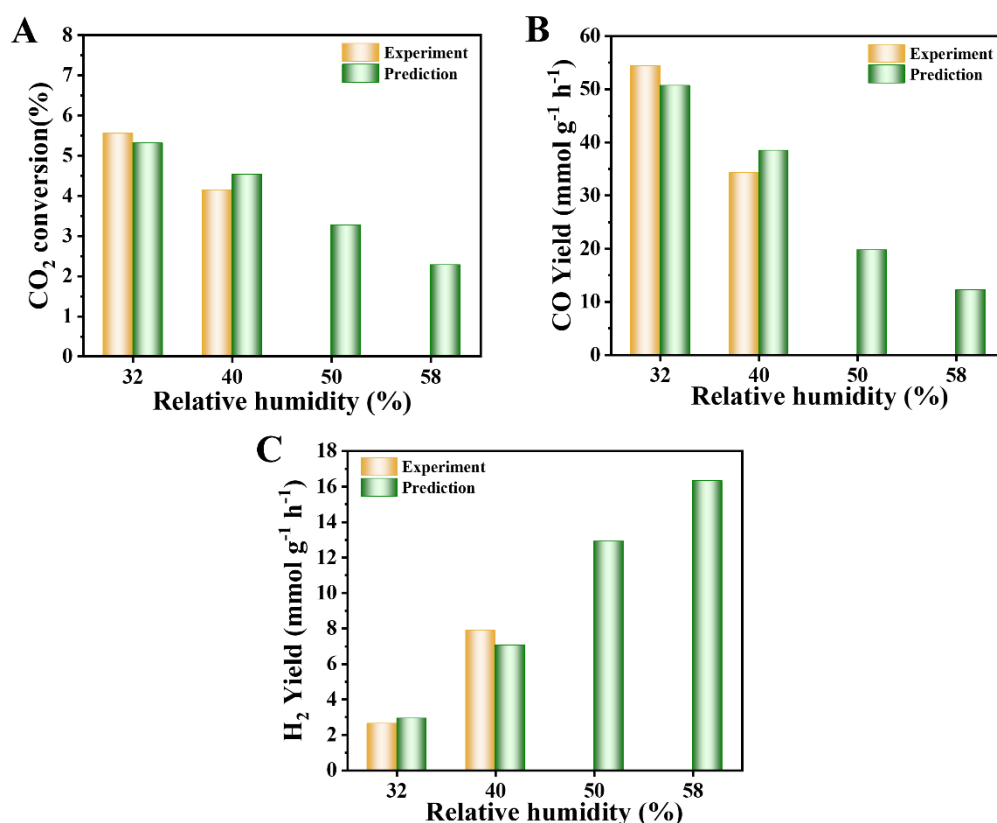
**Supplementary Figure 10.** Infrared thermal images of reactor during reaction under (A) non-reacting conditions, (B) light-only conditions and (C) plasma–light coupling conditions.



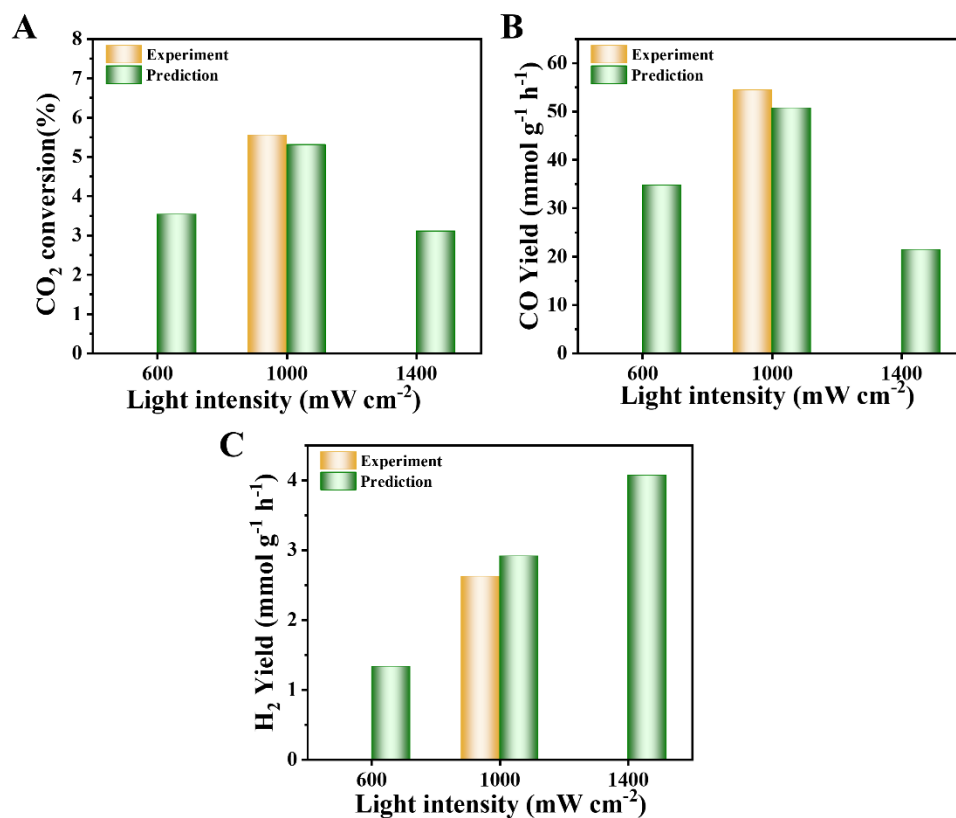
**Supplementary Figure 11.** The correlation matrix graph.

To obtain an initial overview of the relationships among the operating variables and reaction outputs, a Pearson correlation matrix was constructed in Supplementary Figure 11. CO<sub>2</sub> conversion showed a strong positive correlation with CO yield, indicating that CO formation is closely associated with CO<sub>2</sub> conversion in this system. In contrast, CO<sub>2</sub> conversion and CO yield were negatively correlated with H<sub>2</sub> yield and H<sub>2</sub>/CO ratio, suggesting a competitive relationship between CO<sub>2</sub> reduction toward CO and hydrogen evolution. Relative humidity was positively correlated with H<sub>2</sub> yield and H<sub>2</sub>/CO ratio but negatively correlated with CO<sub>2</sub> conversion and CO yield, indicating that increasing water content tends to shift the reaction toward H<sub>2</sub> formation. It should be noted that the correlation matrix only reflects pairwise linear relationships and cannot fully describe nonlinear or coupled effects among variables. For example, discharge power and light intensity may exhibit optimal operating

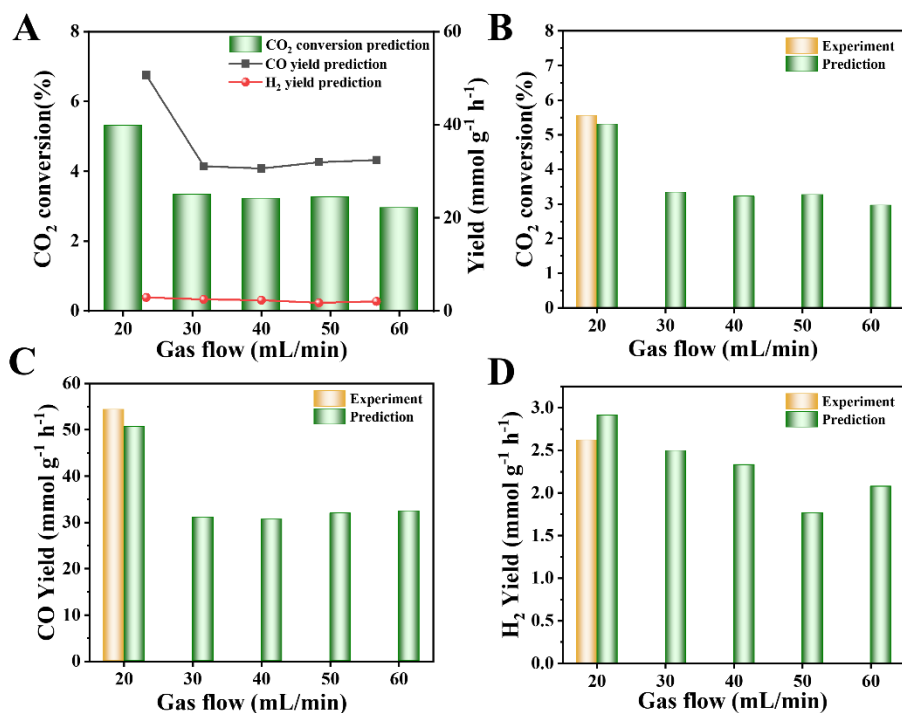
windows rather than monotonic effects, which can lead to weak linear correlations despite their strong influence on reaction performance. Therefore, the correlation analysis was used only as a preliminary description of the dataset, while PFI, SHAP analysis, and response-trend analysis were further employed to reveal nonlinear variable effects and multi-objective competition in the plasma-coupled photocatalytic system.



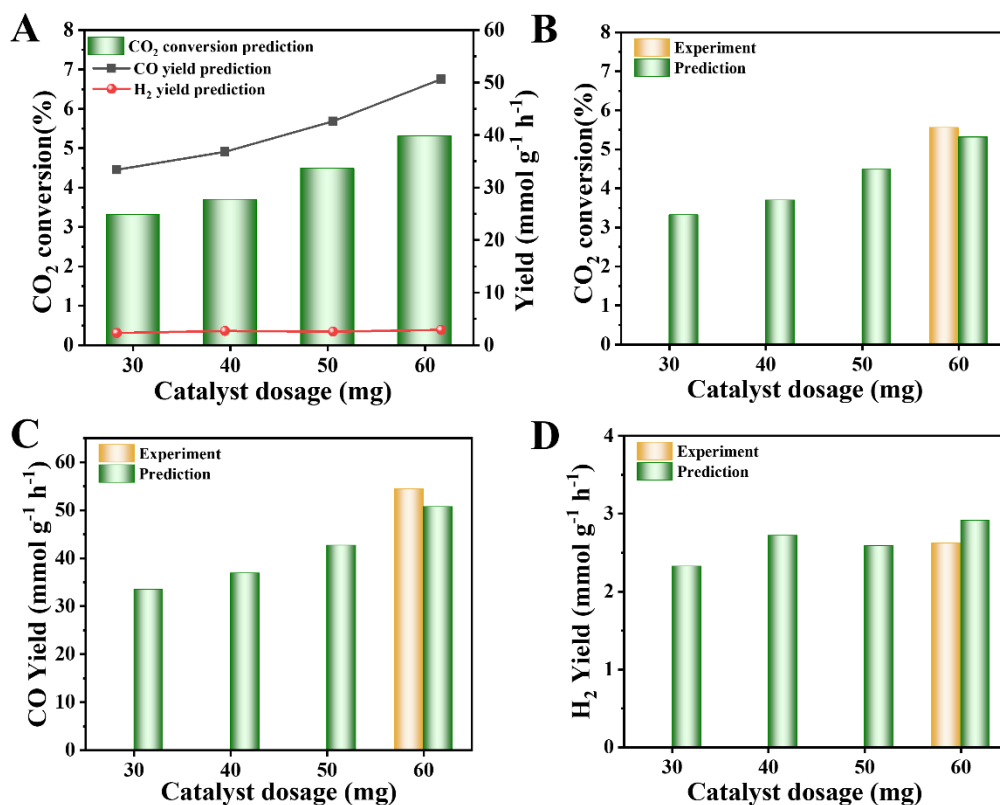
**Supplementary Figure 12.** Correlation between hybrid model prediction and experimental data for the effect of relative humidity on the plasma-photocatalytic CO<sub>2</sub> and H<sub>2</sub>O conversion reaction performance (A) CO<sub>2</sub> conversion, (B) CO yield and (C) H<sub>2</sub> yield (Discharge power: 50 W, light intensity: 1000 mW cm<sup>-2</sup>, gas flow: 20 mL min<sup>-1</sup>, catalyst dosage: 60 mg).



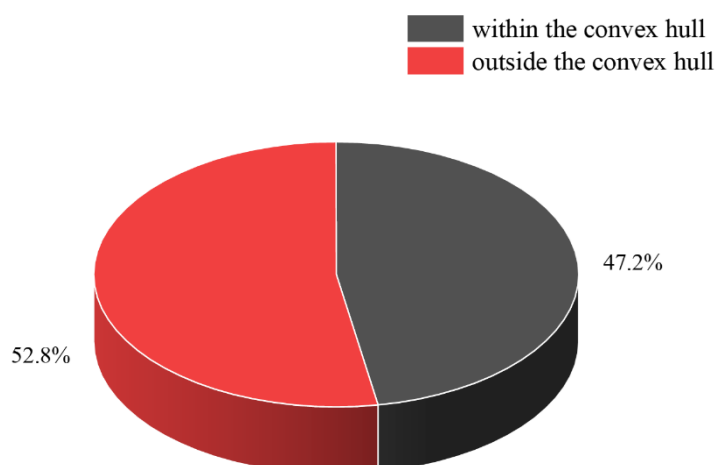
**Supplementary Figure 13.** Correlation between hybrid model prediction and experimental data for the effect of light intensity on the plasma-photocatalytic  $\text{CO}_2$  and  $\text{H}_2\text{O}$  conversion reaction performance (A)  $\text{CO}_2$  conversion, (B) CO yield and (C)  $\text{H}_2$  yield (Discharge power: 50 W, relative humidity: 32 %, gas flow:  $20 \text{ mL min}^{-1}$ , catalyst dosage: 60 mg).



**Supplementary Figure 14.** Predicted effects of (A) gas flow on the plasma-photocatalytic CO<sub>2</sub> and H<sub>2</sub>O conversion reaction performance. Correlation between hybrid model prediction and experimental data for the effect of gas flow on the plasma-photocatalytic CO<sub>2</sub> and H<sub>2</sub>O conversion reaction performance (B) CO<sub>2</sub> conversion, (C) CO yield and (D) H<sub>2</sub> yield (Discharge power: 50 W, light intensity: 1000 mW cm<sup>-2</sup>, relative humidity: 32 %, catalyst dosage: 60 mg).



**Supplementary Figure 15.** Predicted effects of (A) catalyst dosage on the plasma-photocatalytic CO<sub>2</sub> and H<sub>2</sub>O conversion reaction performance. Correlation between hybrid model prediction and experimental data for the effect of catalyst dosage on the plasma-photocatalytic CO<sub>2</sub> and H<sub>2</sub>O conversion reaction performance (B) CO<sub>2</sub> conversion, (C) CO yield and (D) H<sub>2</sub> yield (Discharge power: 50 W, light intensity: 1000 mW cm<sup>-2</sup>, relative humidity: 32 %, gas flow: 20 mL min<sup>-1</sup>).



**Supplementary Figure 16.** Distribution of the 100,000 generated candidate conditions inside and outside the convex hull of the SPXY training set.

**Supplementary Table 1.** The comparison of different catalysts under only-plasma and plasma-light conditions (Discharge power: 60 W, catalysts dose: 30 mg, gas flow: mL min<sup>-1</sup>, relative humidity 50%, light intensity: 1000 mW cm<sup>-2</sup>)

| Catalysts                      | Only plasma conditions         |                                                  |                                                              | Plasma + light conditions      |                                                  |                                                              |
|--------------------------------|--------------------------------|--------------------------------------------------|--------------------------------------------------------------|--------------------------------|--------------------------------------------------|--------------------------------------------------------------|
|                                | CO <sub>2</sub> conversion (%) | CO yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) | H <sub>2</sub> yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) | CO <sub>2</sub> conversion (%) | CO yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) | H <sub>2</sub> yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) |
| CeO <sub>2</sub>               | 0.58±0.08                      | 5.82±0.72                                        | 15.34±2.10                                                   | 0.82±0.10                      | 8.63±1.04                                        | 12.52±1.63                                                   |
| Al <sub>2</sub> O <sub>3</sub> | 0.50±0.07                      | 4.91±0.66                                        | 13.80±1.85                                                   | 0.43±0.06                      | 4.12±0.58                                        | 11.96±1.52                                                   |
| ZSM-5                          | 0.38±0.05                      | 3.55±0.49                                        | 10.70±1.36                                                   | 0.40±0.06                      | 3.71±0.52                                        | 9.95±1.29                                                    |
| TiO <sub>2</sub>               | 0.76±0.09                      | 7.86±0.92                                        | 16.28±2.24                                                   | 1.05±0.13                      | 11.42±1.35                                       | 13.03±1.68                                                   |
| Cu/TiO <sub>2</sub>            | 1.07±0.15                      | 10.95±1.62                                       | 7.12±0.96                                                    | 1.33±0.18                      | 13.82±2.14                                       | 6.96±0.94                                                    |
| Pd/TiO <sub>2</sub>            | 1.24±0.17                      | 11.50±1.86                                       | 8.39±1.12                                                    | 1.06±0.15                      | 10.81±1.71                                       | 10.60±1.48                                                   |
| Cu–Pd/TiO <sub>2</sub>         | 1.40±0.26                      | 13.93±1.94                                       | 24.93±3.28                                                   | 2.86±0.54                      | 28.52±3.96                                       | 18.51±2.93                                                   |

**Supplementary Table 2. Carbon balance of 20 independently experimental runs**

| No. | Carbon balance (%) |
|-----|--------------------|
| 1   | 99.93±0.12         |
| 2   | 99.87±0.15         |
| 3   | 99.83±0.21         |
| 4   | 99.90±0.10         |
| 5   | 99.77±0.25         |
| 6   | 99.80±0.10         |
| 7   | 99.73±0.31         |
| 8   | 99.77±0.15         |
| 9   | 99.90±0.17         |
| 10  | 99.80±0.26         |
| 11  | 99.87±0.12         |
| 12  | 99.77±0.21         |
| 13  | 99.83±0.12         |
| 14  | 99.70±0.20         |
| 15  | 99.80±0.17         |
| 16  | 99.87±0.06         |
| 17  | 99.70±0.30         |
| 18  | 99.87±0.23         |
| 19  | 99.73±0.21         |
| 20  | 99.83±0.15         |

**Supplementary Table 3. Comparison of other state-of-the-art photocatalysts**

| Catalyst                              | CO yield ( $\mu\text{mol g}^{-1} \text{ h}^{-1}$ ) | H <sub>2</sub> yield ( $\mu\text{mol g}^{-1} \text{ h}^{-1}$ ) | Syngas H <sub>2</sub> /CO ratio | Reference |
|---------------------------------------|----------------------------------------------------|----------------------------------------------------------------|---------------------------------|-----------|
| CIS/Co-PBA/NaY-5                      | 306.19                                             | 1152.29                                                        | 3.76:1                          | [3]       |
| 30% ZIF-BT                            | 2486.4                                             | 3495.0                                                         | 1.41:1                          | [4]       |
| 150TiO <sub>2</sub> /CN               | 6200                                               | 1900                                                           | 0.31:1                          | [5]       |
| CdS/BiVO <sub>4</sub> @T-COF          | 183.8                                              | 269.8                                                          | 1.47:1                          | [6]       |
| Zn <sub>0.8</sub> Cd <sub>0.2</sub> S | 680                                                | 1020                                                           | 1.5:1                           | [7]       |
| CdS <sub>1-x</sub> -M                 | 96.18                                              | 569.12 <sup>1</sup>                                            | 6:1                             | [8]       |
| 3 wt% Ni <sub>2</sub> P/CdS           | 50.6                                               | 115                                                            | 2.27:1                          | [9]       |
| Cu-Pd/TiO <sub>2</sub>                | 56420                                              | 53710                                                          | 0.022:1-53.71:1                 | This work |

**Supplementary Table 4. Experimental dataset of plasma-coupled photocatalysis CO<sub>2</sub> and H<sub>2</sub>O conversion reaction**

| NO | Discharge power (W) | Catalysts dose (mg) | Gas flow (mL min <sup>-1</sup> ) | Relative humidity (%) | Light intensity (mW cm <sup>-2</sup> ) |
|----|---------------------|---------------------|----------------------------------|-----------------------|----------------------------------------|
| 1  | 40                  | 60                  | 20                               | 32                    | 1000                                   |
| 2  | 70                  | 30                  | 40                               | 58                    | 1400                                   |
| 3  | 30                  | 30                  | 60                               | 32                    | 1400                                   |
| 4  | 70                  | 50                  | 20                               | 58                    | 600                                    |
| 5  | 60                  | 30                  | 20                               | 32                    | 600                                    |
| 6  | 30                  | 60                  | 60                               | 58                    | 1400                                   |
| 7  | 50                  | 60                  | 30                               | 40                    | 1400                                   |
| 8  | 30                  | 30                  | 50                               | 58                    | 600                                    |
| 9  | 30                  | 50                  | 50                               | 40                    | 1000                                   |
| 10 | 70                  | 40                  | 60                               | 40                    | 1400                                   |
| 11 | 70                  | 50                  | 40                               | 32                    | 600                                    |

## Energy Materials

|    |    |    |    |    |      |
|----|----|----|----|----|------|
| 12 | 70 | 60 | 30 | 50 | 1400 |
| 13 | 30 | 30 | 40 | 58 | 1400 |
| 14 | 60 | 30 | 30 | 50 | 1000 |
| 15 | 30 | 60 | 40 | 50 | 600  |
| 16 | 60 | 60 | 20 | 40 | 1000 |
| 17 | 70 | 60 | 50 | 58 | 1000 |
| 18 | 40 | 40 | 30 | 58 | 1000 |
| 19 | 70 | 60 | 60 | 58 | 1400 |
| 20 | 60 | 40 | 50 | 32 | 1000 |
| 21 | 70 | 30 | 50 | 58 | 600  |
| 22 | 30 | 30 | 20 | 40 | 600  |
| 23 | 50 | 60 | 40 | 40 | 600  |
| 24 | 70 | 50 | 30 | 32 | 1400 |
| 25 | 30 | 50 | 30 | 32 | 1400 |
| 26 | 70 | 30 | 30 | 50 | 1000 |
| 27 | 40 | 40 | 50 | 32 | 1000 |
| 28 | 40 | 60 | 50 | 58 | 1000 |
| 29 | 30 | 60 | 30 | 50 | 1400 |
| 30 | 70 | 30 | 20 | 40 | 600  |
| 31 | 70 | 60 | 20 | 40 | 1000 |
| 32 | 40 | 50 | 20 | 58 | 600  |
| 33 | 30 | 60 | 20 | 40 | 1000 |
| 34 | 40 | 30 | 20 | 32 | 600  |
| 35 | 30 | 30 | 30 | 50 | 1000 |
| 36 | 60 | 50 | 60 | 50 | 1400 |
| 37 | 60 | 60 | 50 | 50 | 1000 |
| 38 | 50 | 40 | 20 | 50 | 600  |
| 39 | 30 | 50 | 40 | 32 | 600  |
| 40 | 50 | 60 | 30 | 50 | 1400 |
| 41 | 70 | 50 | 50 | 40 | 1000 |
| 42 | 60 | 60 | 40 | 50 | 600  |
| 43 | 60 | 30 | 60 | 32 | 1400 |
| 44 | 40 | 40 | 60 | 40 | 1400 |
| 45 | 60 | 40 | 30 | 58 | 1000 |
| 46 | 40 | 60 | 50 | 50 | 1000 |
| 47 | 50 | 60 | 60 | 58 | 1400 |
| 48 | 30 | 50 | 60 | 50 | 1400 |
| 49 | 30 | 60 | 30 | 40 | 1400 |

## Energy Materials

|    |    |    |    |    |      |
|----|----|----|----|----|------|
| 50 | 70 | 60 | 30 | 40 | 1400 |
| 51 | 70 | 60 | 40 | 40 | 600  |
| 52 | 50 | 50 | 30 | 32 | 1400 |
| 53 | 50 | 30 | 40 | 58 | 1400 |
| 54 | 60 | 50 | 50 | 40 | 1000 |
| 55 | 60 | 50 | 40 | 32 | 600  |
| 56 | 30 | 40 | 20 | 50 | 600  |
| 57 | 30 | 60 | 40 | 40 | 600  |
| 58 | 70 | 40 | 20 | 50 | 600  |
| 59 | 70 | 60 | 40 | 50 | 600  |
| 60 | 70 | 40 | 50 | 32 | 1000 |
| 61 | 70 | 60 | 20 | 32 | 1000 |
| 62 | 30 | 60 | 50 | 50 | 1000 |
| 63 | 50 | 30 | 50 | 58 | 600  |
| 64 | 60 | 50 | 20 | 58 | 600  |
| 65 | 30 | 60 | 20 | 32 | 1000 |
| 66 | 60 | 30 | 20 | 40 | 600  |
| 67 | 60 | 30 | 40 | 58 | 1400 |
| 68 | 40 | 50 | 60 | 50 | 1400 |
| 69 | 50 | 50 | 50 | 40 | 1000 |
| 70 | 70 | 30 | 60 | 32 | 1400 |
| 71 | 60 | 40 | 60 | 40 | 1400 |
| 72 | 70 | 60 | 50 | 50 | 1000 |
| 73 | 60 | 60 | 20 | 32 | 1000 |
| 74 | 50 | 40 | 50 | 32 | 1000 |
| 75 | 60 | 40 | 20 | 50 | 600  |
| 76 | 50 | 30 | 20 | 40 | 600  |
| 77 | 40 | 60 | 30 | 50 | 1400 |
| 78 | 30 | 40 | 30 | 58 | 1000 |
| 79 | 60 | 50 | 30 | 32 | 1400 |
| 80 | 40 | 30 | 30 | 50 | 1000 |
| 81 | 60 | 60 | 40 | 40 | 600  |
| 82 | 40 | 50 | 40 | 32 | 600  |
| 83 | 70 | 40 | 30 | 58 | 1000 |
| 84 | 30 | 40 | 50 | 32 | 1000 |
| 85 | 40 | 60 | 20 | 40 | 1000 |
| 86 | 60 | 60 | 30 | 50 | 1400 |
| 87 | 30 | 30 | 20 | 32 | 600  |

## Energy Materials

|     |    |    |    |    |      |
|-----|----|----|----|----|------|
| 88  | 60 | 60 | 60 | 58 | 1400 |
| 89  | 70 | 30 | 20 | 32 | 600  |
| 90  | 70 | 50 | 60 | 50 | 1400 |
| 91  | 50 | 30 | 20 | 32 | 600  |
| 92  | 40 | 30 | 40 | 58 | 1400 |
| 93  | 40 | 60 | 30 | 40 | 1400 |
| 94  | 50 | 50 | 60 | 50 | 1400 |
| 95  | 50 | 60 | 50 | 58 | 1000 |
| 96  | 50 | 40 | 30 | 58 | 1000 |
| 97  | 30 | 50 | 20 | 58 | 600  |
| 98  | 30 | 60 | 50 | 58 | 1000 |
| 99  | 30 | 40 | 60 | 40 | 1400 |
| 100 | 40 | 30 | 20 | 40 | 600  |
| 101 | 40 | 60 | 40 | 40 | 600  |
| 102 | 40 | 40 | 20 | 50 | 600  |
| 103 | 40 | 60 | 40 | 50 | 600  |
| 104 | 40 | 30 | 50 | 58 | 600  |
| 105 | 40 | 50 | 50 | 40 | 1000 |
| 106 | 40 | 50 | 30 | 32 | 1400 |
| 107 | 40 | 30 | 60 | 32 | 1400 |
| 108 | 40 | 60 | 60 | 58 | 1400 |
| 109 | 50 | 50 | 40 | 32 | 600  |
| 110 | 50 | 60 | 40 | 50 | 600  |
| 111 | 50 | 50 | 20 | 58 | 600  |
| 112 | 50 | 60 | 20 | 32 | 1000 |
| 113 | 50 | 60 | 20 | 40 | 1000 |
| 114 | 50 | 30 | 30 | 50 | 1000 |
| 115 | 50 | 60 | 50 | 50 | 1000 |
| 116 | 50 | 30 | 60 | 32 | 1400 |
| 117 | 50 | 40 | 60 | 40 | 1400 |
| 118 | 60 | 30 | 50 | 58 | 600  |
| 119 | 60 | 60 | 50 | 58 | 1000 |
| 120 | 60 | 60 | 30 | 40 | 1400 |

**Supplementary Table 5. Comparison of hybrid model prediction and experimental results**

| No | Model Prediction               |                                                  |                                                              | Actual experiment              |                                                  |                                                              |
|----|--------------------------------|--------------------------------------------------|--------------------------------------------------------------|--------------------------------|--------------------------------------------------|--------------------------------------------------------------|
|    | CO <sub>2</sub> conversion (%) | CO yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) | H <sub>2</sub> yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) | CO <sub>2</sub> conversion (%) | CO yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) | H <sub>2</sub> yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) |
| 1  | 5.38                           | 53.43                                            | 2.68                                                         | 5.52±0.73                      | 56.42±6.10                                       | 2.21±0.26                                                    |
| 2  | 0.45                           | 0.78                                             | 53.47                                                        | 0.43±0.06                      | 1.00±0.14                                        | 53.71±5.19                                                   |
| 3  | 1.59                           | 11.76                                            | 4.19                                                         | 1.54±0.14                      | 10.31±1.28                                       | 4.00±0.54                                                    |
| 4  | 0.87                           | 0.99                                             | 12.75                                                        | 0.85±0.11                      | 1.33±0.15                                        | 13.20±1.41                                                   |
| 5  | 3.10                           | 28.69                                            | 1.92                                                         | 3.17±0.30                      | 27.25±2.68                                       | 2.25±0.36                                                    |
| 6  | 0.72                           | 1.32                                             | 32.67                                                        | 0.81±0.09                      | 1.00±0.12                                        | 32.93±4.07                                                   |
| 7  | 1.98                           | 8.86                                             | 14.83                                                        | 2.15±0.20                      | 9.08±0.82                                        | 15.37±2.03                                                   |
| 8  | 1.04                           | 3.99                                             | 9.97                                                         | 1.13±0.13                      | 4.25±0.55                                        | 9.68±1.20                                                    |
| 9  | 3.23                           | 31.16                                            | 6.94                                                         | 3.25±0.30                      | 31.49±3.42                                       | 7.50±0.62                                                    |
| 10 | 0.75                           | 2.05                                             | 11.95                                                        | 0.70±0.12                      | 2.48±0.29                                        | 12.12±1.08                                                   |
| 11 | 1.97                           | 10.62                                            | 1.74                                                         | 2.09±0.25                      | 9.33±1.08                                        | 1.38±0.20                                                    |
| 12 | 0.64                           | 2.11                                             | 40.27                                                        | 0.57±0.09                      | 1.66±0.17                                        | 41.87±5.01                                                   |
| 13 | 0.56                           | 3.26                                             | 39.41                                                        | 0.39±0.06                      | 3.30±0.42                                        | 40.47±4.14                                                   |
| 14 | 2.57                           | 24.28                                            | 18.07                                                        | 2.86±0.54                      | 28.52±3.96                                       | 18.51±2.93                                                   |
| 15 | 1.90                           | 9.31                                             | 7.84                                                         | 2.00±0.19                      | 9.91±0.81                                        | 8.32±0.97                                                    |
| 16 | 4.09                           | 31.13                                            | 7.40                                                         | 4.17±0.51                      | 31.92±3.55                                       | 6.12±0.60                                                    |
| 17 | 0.93                           | 2.36                                             | 25.63                                                        | 0.83±0.11                      | 2.73±0.42                                        | 26.47±3.74                                                   |
| 18 | 2.01                           | 12.28                                            | 18.74                                                        | 2.04±0.20                      | 11.99±1.12                                       | 18.82±2.62                                                   |
| 19 | 0.22                           | 0.81                                             | 50.79                                                        | 0.28±0.04                      | 1.00±0.12                                        | 51.99±5.88                                                   |
| 20 | 3.31                           | 35.88                                            | 2.60                                                         | 3.26±0.40                      | 36.93±2.92                                       | 2.37±0.33                                                    |
| 21 | 0.55                           | 0.99                                             | 12.82                                                        | 0.55±0.07                      | 1.74±0.25                                        | 13.12±1.88                                                   |
| 22 | 2.82                           | 22.96                                            | 3.87                                                         | 2.61±0.25                      | 21.00±2.33                                       | 4.58±0.52                                                    |
| 23 | 2.94                           | 21.09                                            | 4.71                                                         | 3.05±0.42                      | 21.14±2.54                                       | 5.87±0.57                                                    |
| 24 | 1.35                           | 3.64                                             | 6.64                                                         | 1.28±0.13                      | 3.62±0.46                                        | 6.66±0.79                                                    |
| 25 | 2.42                           | 14.03                                            | 4.04                                                         | 2.32±0.25                      | 12.93±1.18                                       | 4.79±0.69                                                    |
| 26 | 1.35                           | 8.91                                             | 18.20                                                        | 1.17±0.14                      | 5.28±0.46                                        | 18.11±1.49                                                   |
| 27 | 4.01                           | 48.52                                            | 2.56                                                         | 4.06±0.58                      | 52.41±5.30                                       | 3.21±0.42                                                    |
| 28 | 1.67                           | 7.99                                             | 16.18                                                        | 1.54±0.14                      | 4.99±0.44                                        | 16.92±2.43                                                   |
| 29 | 1.43                           | 5.39                                             | 24.69                                                        | 1.68±0.24                      | 6.59±0.72                                        | 25.02±3.39                                                   |
| 30 | 1.66                           | 9.78                                             | 4.00                                                         | 1.78±0.20                      | 10.48±1.16                                       | 3.70±0.41                                                    |

## Energy Materials

|    |      |       |       |           |            |            |
|----|------|-------|-------|-----------|------------|------------|
| 31 | 2.53 | 13.20 | 8.12  | 2.31±0.31 | 10.95±1.14 | 9.24±0.94  |
| 32 | 1.53 | 9.82  | 8.57  | 1.33±0.16 | 8.26±0.66  | 7.89±1.09  |
| 33 | 4.57 | 38.40 | 7.12  | 4.57±0.58 | 38.18±4.81 | 7.49±0.63  |
| 34 | 3.61 | 37.84 | 1.21  | 3.77±0.47 | 40.16±4.48 | 0.88±0.12  |
| 35 | 2.62 | 24.95 | 12.11 | 2.55±0.37 | 25.47±3.23 | 11.87±1.69 |
| 36 | 0.81 | 3.02  | 32.07 | 0.69±0.09 | 2.57±0.31  | 30.88±3.12 |
| 37 | 2.21 | 12.01 | 16.52 | 2.23±0.23 | 11.36±1.36 | 17.51±2.46 |
| 38 | 2.33 | 16.26 | 7.02  | 2.39±0.30 | 17.01±1.29 | 5.70±0.51  |
| 39 | 3.18 | 27.68 | 1.21  | 3.20±0.46 | 26.46±3.22 | 0.80±0.12  |
| 40 | 1.30 | 5.86  | 32.91 | 1.25±0.12 | 8.29±1.09  | 35.62±4.72 |
| 41 | 2.16 | 14.27 | 7.32  | 2.18±0.24 | 13.02±1.17 | 7.41±0.71  |
| 42 | 1.95 | 8.82  | 9.09  | 1.97±0.19 | 8.83±0.88  | 8.63±1.04  |
| 43 | 1.28 | 7.66  | 4.13  | 1.19±0.17 | 6.93±0.61  | 4.34±0.49  |
| 44 | 1.35 | 6.25  | 12.44 | 1.31±0.13 | 5.40±0.72  | 12.52±1.78 |
| 45 | 1.64 | 9.90  | 25.22 | 1.56±0.17 | 9.16±1.11  | 26.11±2.45 |
| 46 | 2.55 | 15.64 | 12.23 | 2.64±0.28 | 17.84±1.61 | 10.51±0.86 |
| 47 | 0.44 | 1.45  | 37.24 | 0.28±0.04 | 1.00±0.16  | 36.88±4.65 |
| 48 | 0.97 | 4.56  | 24.67 | 1.06±0.12 | 6.09±0.60  | 23.91±2.41 |
| 49 | 1.81 | 8.30  | 11.00 | 1.68±0.17 | 7.29±0.77  | 10.38±0.97 |
| 50 | 1.17 | 3.30  | 16.93 | 1.32±0.16 | 4.83±0.61  | 16.58±2.14 |
| 51 | 1.48 | 5.47  | 4.81  | 1.29±0.16 | 4.26±0.42  | 4.07±0.58  |
| 52 | 2.64 | 13.56 | 3.72  | 2.77±0.38 | 12.63±1.57 | 1.36±0.20  |
| 53 | 0.90 | 3.74  | 40.77 | 0.91±0.15 | 4.55±0.55  | 38.79±4.95 |
| 54 | 3.03 | 26.98 | 7.29  | 2.98±0.40 | 28.57±3.42 | 6.98±0.87  |
| 55 | 3.10 | 25.13 | 1.52  | 3.02±0.38 | 24.54±2.53 | 0.80±0.12  |
| 56 | 2.18 | 12.76 | 6.56  | 2.28±0.29 | 12.49±1.51 | 6.60±0.83  |
| 57 | 2.51 | 18.10 | 3.61  | 2.41±0.28 | 17.90±1.45 | 2.66±0.29  |
| 58 | 1.28 | 3.26  | 9.38  | 1.41±0.14 | 3.37±0.28  | 8.75±1.02  |
| 59 | 1.03 | 1.40  | 11.15 | 0.91±0.12 | 2.15±0.26  | 12.89±1.23 |
| 60 | 2.18 | 17.73 | 2.53  | 2.07±0.27 | 14.09±1.36 | 1.73±0.24  |
| 61 | 2.90 | 16.65 | 3.56  | 2.96±0.34 | 17.10±1.65 | 2.59±0.30  |
| 62 | 2.11 | 10.52 | 12.81 | 1.92±0.23 | 8.68±1.09  | 13.62±1.21 |
| 63 | 1.19 | 5.12  | 9.63  | 1.08±0.10 | 3.69±0.40  | 9.75±1.04  |
| 64 | 1.67 | 7.04  | 11.51 | 1.80±0.20 | 6.38±0.61  | 11.82±1.50 |
| 65 | 5.03 | 47.36 | 2.93  | 5.01±0.68 | 46.69±4.33 | 3.16±0.38  |
| 66 | 2.78 | 21.28 | 4.10  | 2.69±0.31 | 20.94±2.58 | 3.75±0.48  |
| 67 | 0.91 | 4.06  | 48.34 | 1.10±0.12 | 4.94±0.56  | 49.32±5.14 |
| 68 | 0.82 | 3.11  | 29.30 | 0.65±0.08 | 1.46±0.21  | 29.88±2.58 |

## Energy Materials

|     |      |       |       |           |            |            |
|-----|------|-------|-------|-----------|------------|------------|
| 69  | 3.39 | 31.58 | 6.69  | 3.64±0.31 | 33.87±3.03 | 7.17±1.03  |
| 70  | 0.49 | 2.28  | 5.12  | 0.50±0.08 | 2.32±0.35  | 5.26±0.62  |
| 71  | 1.34 | 4.74  | 10.48 | 1.44±0.18 | 4.69±0.40  | 9.86±1.30  |
| 72  | 1.51 | 4.60  | 17.93 | 1.66±0.19 | 5.27±0.52  | 17.12±1.52 |
| 73  | 4.49 | 36.71 | 3.54  | 4.54±0.40 | 37.28±3.29 | 4.42±0.39  |
| 74  | 3.78 | 42.98 | 2.39  | 3.86±0.45 | 44.01±3.94 | 2.83±0.30  |
| 75  | 2.07 | 12.43 | 8.54  | 1.91±0.19 | 12.18±1.01 | 9.89±1.00  |
| 76  | 3.03 | 27.17 | 3.66  | 3.02±0.41 | 28.72±3.85 | 3.70±0.31  |
| 77  | 1.26 | 5.43  | 29.50 | 1.18±0.13 | 2.46±0.39  | 28.88±2.98 |
| 78  | 1.87 | 10.26 | 13.37 | 1.94±0.28 | 10.56±1.11 | 11.52±1.33 |
| 79  | 2.33 | 11.42 | 5.37  | 2.36±0.21 | 12.63±1.17 | 7.06±0.66  |
| 80  | 2.95 | 27.87 | 13.91 | 3.13±0.34 | 28.82±3.42 | 13.96±1.16 |
| 81  | 2.58 | 16.28 | 4.41  | 2.63±0.24 | 15.39±1.31 | 3.98±0.46  |
| 82  | 3.47 | 31.57 | 1.93  | 3.49±0.46 | 33.04±4.12 | 2.90±0.38  |
| 83  | 1.08 | 3.39  | 26.44 | 1.07±0.11 | 4.43±0.41  | 27.04±2.49 |
| 84  | 3.76 | 44.86 | 2.21  | 3.88±0.52 | 45.45±4.20 | 2.43±0.41  |
| 85  | 4.87 | 43.61 | 6.94  | 4.95±0.72 | 43.75±5.83 | 7.49±0.98  |
| 86  | 1.14 | 5.39  | 33.99 | 1.06±0.15 | 4.12±0.37  | 30.88±3.02 |
| 87  | 3.39 | 33.80 | 1.34  | 3.44±0.30 | 34.43±2.68 | 1.09±0.18  |
| 88  | 0.43 | 2.13  | 42.59 | 0.35±0.05 | 2.70±0.31  | 42.70±4.03 |
| 89  | 1.79 | 14.33 | 1.86  | 1.66±0.24 | 14.16±1.26 | 1.77±0.25  |
| 90  | 0.44 | 1.87  | 36.29 | 0.49±0.06 | 3.24±0.41  | 36.04±3.76 |
| 91  | 3.54 | 36.04 | 1.53  | 3.48±0.45 | 35.54±4.78 | 1.84±0.26  |
| 92  | 0.82 | 3.24  | 41.36 | 0.82±0.09 | 1.20±0.14  | 42.20±4.86 |
| 93  | 1.79 | 9.01  | 13.54 | 1.61±0.21 | 9.89±0.93  | 13.88±1.67 |
| 94  | 0.93 | 2.24  | 29.77 | 1.07±0.10 | 1.00±0.12  | 30.78±3.60 |
| 95  | 1.61 | 8.48  | 18.39 | 1.72±0.15 | 9.13±0.75  | 17.11±2.28 |
| 96  | 1.85 | 10.82 | 21.94 | 1.79±0.23 | 10.56±1.07 | 21.84±3.04 |
| 97  | 1.39 | 7.04  | 7.99  | 1.61±0.18 | 9.45±1.18  | 10.56±1.35 |
| 98  | 1.35 | 3.22  | 15.68 | 1.55±0.21 | 6.75±0.68  | 13.35±1.19 |
| 99  | 1.30 | 7.32  | 10.32 | 1.16±0.14 | 6.76±0.91  | 12.00±1.11 |
| 100 | 3.00 | 27.61 | 3.49  | 2.86±0.27 | 26.00±2.22 | 4.32±0.38  |
| 101 | 2.87 | 21.06 | 4.06  | 2.87±0.27 | 20.55±1.75 | 2.81±0.36  |
| 102 | 2.31 | 16.18 | 6.46  | 2.41±0.34 | 17.20±1.40 | 5.56±0.73  |
| 103 | 2.24 | 11.94 | 7.45  | 2.08±0.22 | 9.33±1.16  | 8.53±1.10  |
| 104 | 1.15 | 5.63  | 9.75  | 1.05±0.13 | 1.97±0.20  | 9.69±1.14  |
| 105 | 3.56 | 35.10 | 6.76  | 3.57±0.51 | 35.95±2.70 | 5.41±0.67  |
| 106 | 2.52 | 14.64 | 3.92  | 2.05±0.27 | 12.74±1.70 | 5.63±0.52  |

## Energy Materials

|     |      |       |       |           |            |            |
|-----|------|-------|-------|-----------|------------|------------|
| 107 | 1.65 | 11.77 | 4.64  | 1.31±0.12 | 8.45±0.84  | 6.58±0.79  |
| 108 | 0.43 | 0.99  | 35.12 | 0.46±0.06 | 1.67±0.23  | 36.15±3.18 |
| 109 | 3.47 | 31.34 | 1.89  | 3.31±0.30 | 30.00±2.98 | 2.11±0.23  |
| 110 | 2.29 | 12.27 | 8.12  | 2.15±0.31 | 12.54±1.51 | 8.72±0.82  |
| 111 | 1.75 | 9.88  | 9.50  | 1.55±0.20 | 5.08±0.53  | 7.68±0.79  |
| 112 | 5.06 | 48.03 | 3.01  | 5.55±0.52 | 54.39±6.76 | 2.62±0.42  |
| 113 | 4.61 | 40.31 | 6.86  | 4.14±0.52 | 34.28±3.08 | 7.89±0.72  |
| 114 | 2.91 | 26.75 | 15.53 | 3.30±0.32 | 31.72±3.93 | 14.11±1.30 |
| 115 | 2.48 | 14.42 | 13.67 | 2.46±0.33 | 14.34±1.92 | 10.84±1.25 |
| 116 | 1.68 | 10.28 | 3.65  | 1.43±0.21 | 7.57±0.79  | 2.99±0.47  |
| 117 | 1.50 | 5.13  | 10.86 | 1.41±0.13 | 6.10±0.54  | 12.62±1.65 |
| 118 | 1.10 | 4.67  | 11.40 | 0.81±0.09 | 3.56±0.43  | 13.23±1.19 |
| 119 | 1.42 | 7.29  | 22.83 | 0.88±0.15 | 4.80±0.47  | 26.06±2.46 |
| 120 | 1.85 | 7.80  | 14.27 | 1.51±0.22 | 4.89±0.40  | 13.58±1.44 |

**Supplementary Table 6. 10 sets unseen reaction conditions**

| No. | Discharge<br>Power (W) | Catalysts<br>Dosage (mg) | Gas Flow<br>(mL min <sup>-1</sup> ) | Relative<br>Humidity (%) | Light<br>Intensity<br>(mW cm <sup>-2</sup> ) |
|-----|------------------------|--------------------------|-------------------------------------|--------------------------|----------------------------------------------|
| 1   | 30                     | 60                       | 30                                  | 46                       | 650                                          |
| 2   | 65                     | 30                       | 60                                  | 40                       | 1350                                         |
| 3   | 70                     | 55                       | 20                                  | 54                       | 1300                                         |
| 4   | 30                     | 35                       | 30                                  | 56                       | 1400                                         |
| 5   | 65                     | 30                       | 25                                  | 36                       | 650                                          |
| 6   | 30                     | 30                       | 60                                  | 46                       | 650                                          |
| 7   | 30                     | 60                       | 60                                  | 40                       | 1400                                         |
| 8   | 60                     | 55                       | 60                                  | 56                       | 850                                          |
| 9   | 45                     | 45                       | 20                                  | 33                       | 1300                                         |
| 10  | 35                     | 30                       | 20                                  | 53                       | 600                                          |

**Supplementary Table 7. Comparison of hybrid model prediction and experimental results over 10 sets unseen reaction conditions**

| No. | Model Prediction               |                                                  |                                                              | Actual experiment              |                                                  |                                                              |
|-----|--------------------------------|--------------------------------------------------|--------------------------------------------------------------|--------------------------------|--------------------------------------------------|--------------------------------------------------------------|
|     | CO <sub>2</sub> conversion (%) | CO yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) | H <sub>2</sub> yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) | CO <sub>2</sub> conversion (%) | CO yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) | H <sub>2</sub> yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) |
|     |                                |                                                  |                                                              |                                |                                                  |                                                              |
| 1   | 2.1                            | 12.65                                            | 6.19                                                         | 2.43±0.08                      | 13.87±0.34                                       | 6.65±0.21                                                    |
| 2   | 0.94                           | 3.51                                             | 11.38                                                        | 1.27±0.05                      | 5.71±0.21                                        | 12.36±0.20                                                   |
| 3   | 0.71                           | 1.65                                             | 27.18                                                        | 1.06±0.05                      | 1.39±0.08                                        | 30.38±0.63                                                   |
| 4   | 0.95                           | 3.71                                             | 30.97                                                        | 0.87±0.04                      | 2.78±0.10                                        | 33.16±0.78                                                   |
| 5   | 2.65                           | 22.57                                            | 2.3                                                          | 3.00±0.07                      | 20.00±0.31                                       | 3.20±0.10                                                    |
| 6   | 1.49                           | 8                                                | 7.47                                                         | 1.19±0.05                      | 10.02±0.18                                       | 8.81±0.21                                                    |
| 7   | 1.24                           | 7.23                                             | 10.99                                                        | 1.12±0.04                      | 9.81±0.20                                        | 12.05±0.23                                                   |
| 8   | 1.32                           | 9.11                                             | 14.28                                                        | 1.59±0.06                      | 8.14±0.18                                        | 15.82±0.25                                                   |
| 9   | 2.92                           | 20.68                                            | 3.72                                                         | 3.10±0.07                      | 19.27±0.38                                       | 3.00±0.11                                                    |
| 10  | 1.97                           | 11.78                                            | 6.78                                                         | 1.70±0.06                      | 13.26±0.25                                       | 8.89±0.21                                                    |

**Supplementary Table 8. Performance of models of absolute production rate**

| Output                                       | Dataset | R <sup>2</sup> | MAE   | RMSE  |
|----------------------------------------------|---------|----------------|-------|-------|
| CO yield (mmol h <sup>-1</sup> )             | Train   | 0.992          | 0.046 | 0.062 |
|                                              | Test    | 0.952          | 0.119 | 0.162 |
| H <sub>2</sub> yield (mmol h <sup>-1</sup> ) | Train   | 0.992          | 0.046 | 0.062 |
|                                              | Test    | 0.960          | 0.071 | 0.093 |

The absolute CO and H<sub>2</sub> production rates were calculated by multiplying the mass-normalized yield by the catalyst mass in grams: absolute production rate = mass-normalized yield × catalyst mass. CO<sub>2</sub> conversion was retained in its original percentage form because it was not normalized by catalyst mass. The same input variables, SPXY data split, and hybrid modelling procedure were used for the additional models. The results are summarized in Supplementary Table 8. The test-set R<sup>2</sup> values of the absolute-rate models were 0.952 for CO and 0.960 for H<sub>2</sub>, which were comparable to those of the corresponding mass-normalized yield models (0.950

and 0.954 in Figure 3B and C, respectively). These results indicate that the main predictive relationships were not solely caused by catalyst-mass normalization. Because the mass-normalized and absolute outputs have different units, their MAE and RMSE values should not be directly compared. The mass-normalized yields were retained as the primary outputs for the main analysis.

**Supplementary Table 9. Model-predicted low–high pairwise interaction contrasts among the operating variables for CO<sub>2</sub> conversion, CO yield and H<sub>2</sub> yield**

| Variable pair                       | CO <sub>2</sub> conversion (%) | CO yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) | H <sub>2</sub> yield (mmol g <sup>-1</sup> h <sup>-1</sup> ) |
|-------------------------------------|--------------------------------|--------------------------------------------------|--------------------------------------------------------------|
| Discharge power × catalyst dosage   | 0.43                           | 8.15                                             | 0.18                                                         |
| Discharge power × gas flow          | 0.78                           | 7.66                                             | −1.14                                                        |
| Discharge power × relative humidity | 0.91                           | 18.48                                            | 10.91                                                        |
| Discharge power × light intensity   | 0.34                           | 4.44                                             | 2.31                                                         |
| Catalyst dosage × gas flow          | −1.16                          | −7.21                                            | −2.24                                                        |
| Catalyst dosage × relative humidity | 0.11                           | 1.71                                             | −1.62                                                        |
| Catalyst dosage × light intensity   | −0.51                          | −2.30                                            | −0.38                                                        |
| Gas flow × relative humidity        | −0.14                          | −4.33                                            | 0.79                                                         |
| Gas flow × light intensity          | 0.30                           | 1.38                                             | 1.69                                                         |
| Relative humidity × light intensity | 0.25                           | 11.04                                            | 27.44                                                        |

The low–high screening results in Supplementary Table 9 showed that the conditional effects depended on both the selected variable pair and the reaction output. The discharge power–relative humidity pair exhibited positive interaction contrasts for CO<sub>2</sub> conversion, CO yield, and H<sub>2</sub> yield, with values of 0.91%, 18.48 mmol g<sup>-1</sup> h<sup>-1</sup>, and 10.91 mmol g<sup>-1</sup> h<sup>-1</sup>, respectively. This indicates that the effect of discharge power depends on the humidity level, possibly because plasma energy input and water loading jointly influence the reaction environment. The relative humidity–light intensity pair showed the strongest conditional interaction for H<sub>2</sub> yield, with an interaction contrast of 27.44 mmol g<sup>-1</sup> h<sup>-1</sup>, compared with 11.04 mmol g<sup>-1</sup> h<sup>-1</sup> for CO yield and 0.25% for CO<sub>2</sub> conversion. This output-dependent behaviour may reflect the coupled influence of water availability and photocatalyst excitation on hydrogen

formation. The formation of H<sub>2</sub> may be more sensitive to the combined effect of these two variables in this P<sup>2</sup>CR system. The catalyst dosage–gas flow rate pair produced negative interaction contrasts for all three outputs, including –1.16% for CO<sub>2</sub> conversion and –7.21 mmol g<sup>–1</sup> h<sup>–1</sup> for CO yield. This behaviour may be associated with the shortened residence time at higher flow rates, which can limit the utilization of additional catalytic surface sites. The discharge power–gas flow rate and gas flow rate–relative humidity pairs exhibited different interaction directions among the three outputs. This observation is consistent with the competing effects of plasma energy input, residence time, reactant throughput, and water-vapor supply. Overall, these results indicate that the operating variables form a coupled input space and that the effect of one variable can depend on the level of another. The interaction contrasts represent model-predicted conditional relationships and should not be interpreted as direct evidence of specific elementary reaction mechanisms.

**Supplementary Table 10. Recommended reaction conditions of trained hybrid model with H<sub>2</sub>/CO target of 1 and 2**

| H <sub>2</sub> /CO target | Discharge Power (W) | Catalysts Dose (mg) | Gas Flow (mL/min) | Relative Humidity (%) | Light Intensity (mW cm <sup>–2</sup> ) |
|---------------------------|---------------------|---------------------|-------------------|-----------------------|----------------------------------------|
| 1                         | 44                  | 33                  | 35                | 51                    | 1121                                   |
| 2                         | 57                  | 39                  | 34                | 54                    | 1119                                   |

**Supplementary Table 11. Comparison of hybrid model prediction and experimental results over recommended reaction conditions with H<sub>2</sub>/CO target of 1 and 2**

| H <sub>2</sub> /CO target | Model prediction           |          |                      |                    | Experimental results       |            |                      |                    |
|---------------------------|----------------------------|----------|----------------------|--------------------|----------------------------|------------|----------------------|--------------------|
|                           | CO <sub>2</sub> conversion | CO yield | H <sub>2</sub> yield | H <sub>2</sub> /CO | CO <sub>2</sub> conversion | CO yield   | H <sub>2</sub> yield | H <sub>2</sub> /CO |
| 1                         | 2.64                       | 20.56    | 21.49                | 1.05               | 2.75±0.02                  | 21.99±1.18 | 23.29±1.03           | 1.06±0.03          |
| 2                         | 2.13                       | 13.15    | 26.32                | 2.00               | 2.25±0.03                  | 14.26±0.51 | 28.33±1.14           | 1.99±0.07          |

**Supplementary Table 12. CO productivity per plasma power over recommended reaction conditions with H<sub>2</sub>/CO target of 1 and 2**

| H <sub>2</sub> /CO target | Power (W) | Catalyst dosage (g) | CO productivity per plasma power (mmol kWh <sup>-1</sup> ) |
|---------------------------|-----------|---------------------|------------------------------------------------------------|
| 1                         | 44        | 0.033               | 16.5±0.9                                                   |
| 2                         | 57        | 0.039               | 9.8±0.3                                                    |

To provide an energy-related descriptor for the recommended conditions, the CO productivity normalized by plasma discharge power was calculated as

$$CO_{power-normalized} = \frac{Y_{CO} \times m_{catalyst}}{P} \quad (4)$$

$Y_{CO}$  is the experimentally measured CO yield (mmol g<sup>-1</sup> h<sup>-1</sup>),  $m_{catalyst}$  is the catalyst mass (g), and  $P$  is the plasma power (kW). The resulting unit is mmol kWh<sup>-1</sup>.

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