

Supplementary Materials

Enhanced strength and ductility of high-entropy alloy via dislocation-mediated heterogeneous martensitic transformation

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Strengthening contribution

In the partially recrystallized Fe₄₀Co₂₀Cr₂₀Mn₁₀Ni₁₀ (at. %) high-entropy alloys (HEAs), the yield strength (σ_y) can be expressed as the sum of multiple strengthening effects of lattice friction stress (σ_0), grain boundary strengthening (σ_{gr}) and dislocation strengthening (σ_{dis}), as follows:

$$\sigma_y = \sigma_0 + \sigma_{gr} + \sigma_{dis} \quad (1)$$

By plotting the Hall-Petch relation, the contribution of σ_0 is 140 MPa^[1]. And grain boundary strengthening can be described as^[2]:

$$\sigma_{gr} = f_{RX}k/\sqrt{d} + f_{NRX}k/\sqrt{d} \quad (2)$$

where $f_{RX} = 74\%$ is the volume fraction of the recrystallized regions, $f_{NRX} = 26\%$ is the volume fraction of the recrystallized regions, $k = 564 \text{ MPa}\cdot\mu\text{m}^{1/2}$ is the Hall-Petch coefficient^[1], and $d = 2 \mu\text{m}$ is the grain size of the recrystallized regions.

Thus, the strength provided by grain boundary is 324 MPa.

The dislocation strengthening is represented by the Taylor hardening law^[3]:

$$\sigma_{dis} = M\alpha Gb\sqrt{\rho_{dis}} \quad (3)$$

where $M = 3.06$ is the Taylor factor, $\alpha = 0.2$ is a constant, $G = 76 \text{ GPa}$ is the shear modulus, $b = 0.26 \text{ nm}$ is the magnitude of the Burgers vector, and ρ_{dis} is the dislocation density, which can be expressed as^[4]:

$$\rho_{dis} = 2\theta/\mu b \quad (4)$$

where $\theta = 0.43$ is the misorientation angle measured from kernel average misorientation maps and $\mu = 10^{-5} \text{ m}$ is the unit length. Based on the calculated dislocation density of $\rho_{dis} = 3.3 \times 10^{14} \text{ m}^{-2}$, the strengthening effect of dislocations (σ_{dis}) is evaluated as 219 MPa. The theoretically predicted $\sigma_y = 683 \text{ MPa}$ agrees well with the measured yield strength of 684 MPa.

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