

Supplementary Materials

Graphene-based flexible magnetic tactile sensor with vertically periodic magnetization for enhanced spatial resolution

Xuejiao Li^{1,#}, Wenwei Gao^{1,#}, Biyan Wang¹, Wenlong Jiao², Hong Su³, Wenbiao Zhou¹, Huikai Xie^{1,2}, Yajing Shen^{4,*}, Xiaoyi Wang^{1,2,*}

¹The School of Integrated Circuits and Electronics, Beijing Institute of Technology, Beijing 100081, China.

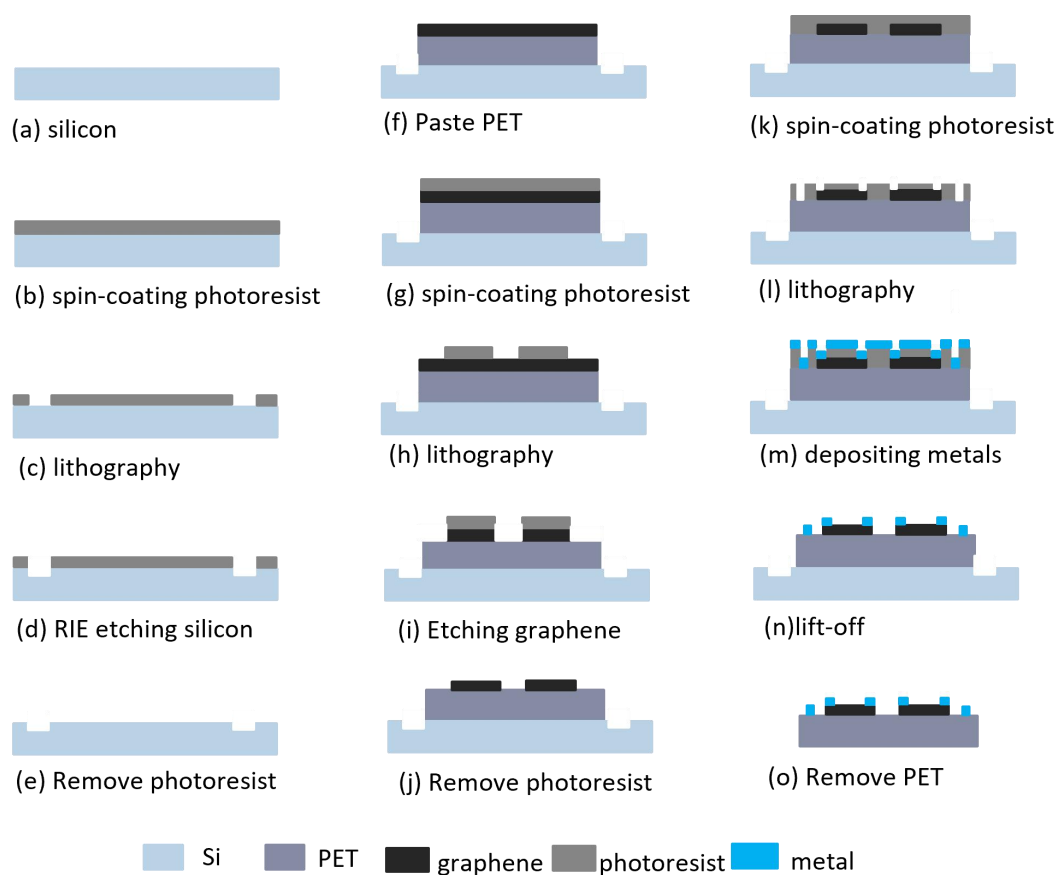
²BIT Chongqing Institute of Microelectronics and Microsystems, Chongqing 400030, China.

³Scientific Research Department, Peking University School and Hospital of Stomatology, Beijing 100081, China.

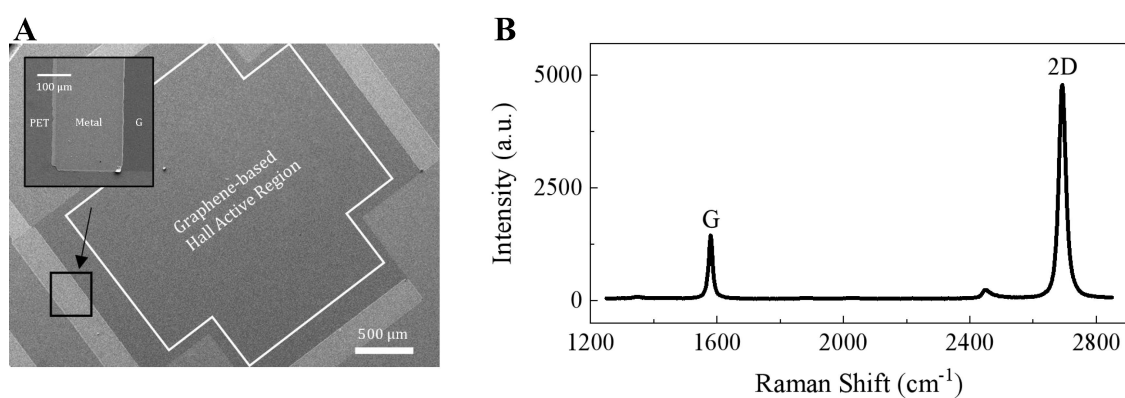
⁴Department of Electronic and Computer Engineering, The Hong Kong University of Science and Technology, Hong Kong 999077, China.

[#]These authors contributed equally to this work.

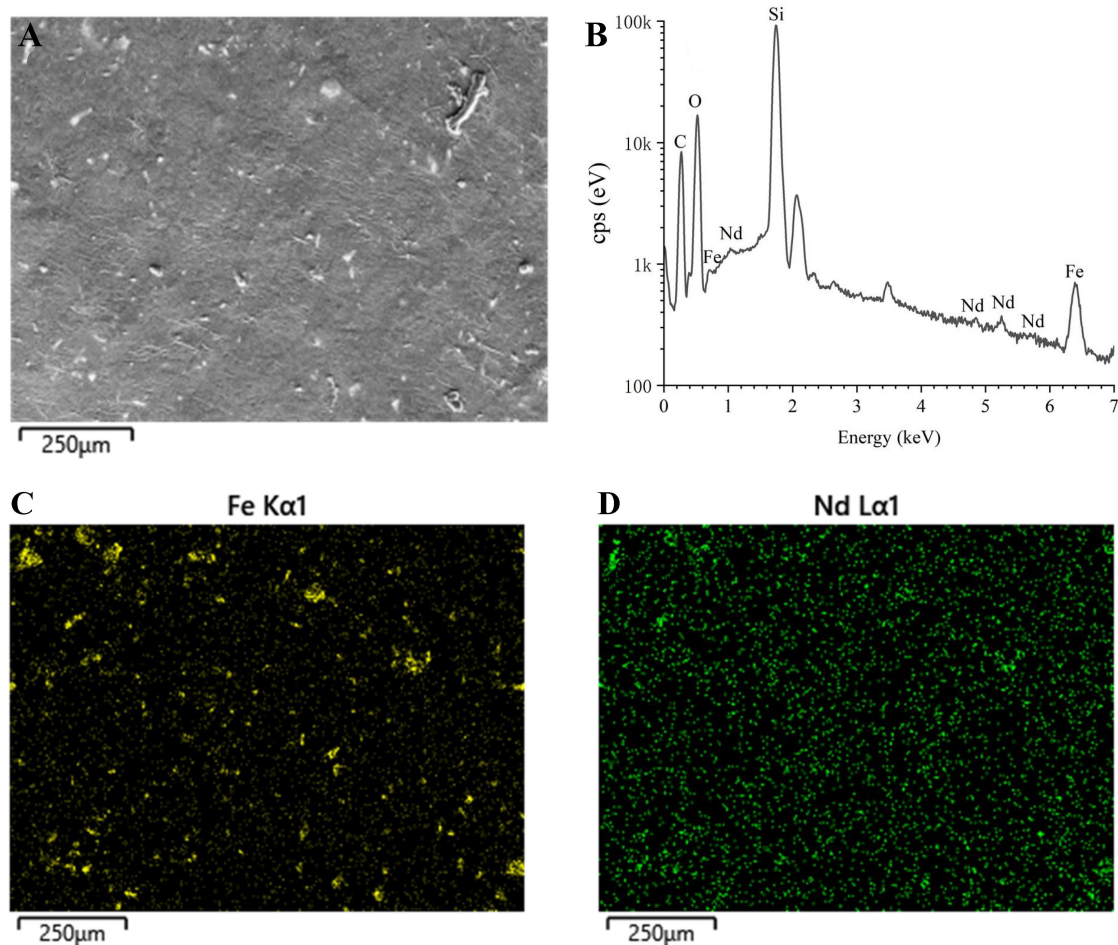
***Correspondence to:** Prof. Yajing Shen, Department of Electronic and Computer Engineering, The Hong Kong University of Science and Technology, Hong Kong 999077, China. E-mail: eeyajing@ust.hk; Prof. Xiaoyi Wang, The School of Integrated Circuits and Electronics, Beijing Institute of Technology, Beijing 100081, China. E-mail: xiaoyiwang@bit.edu.cn



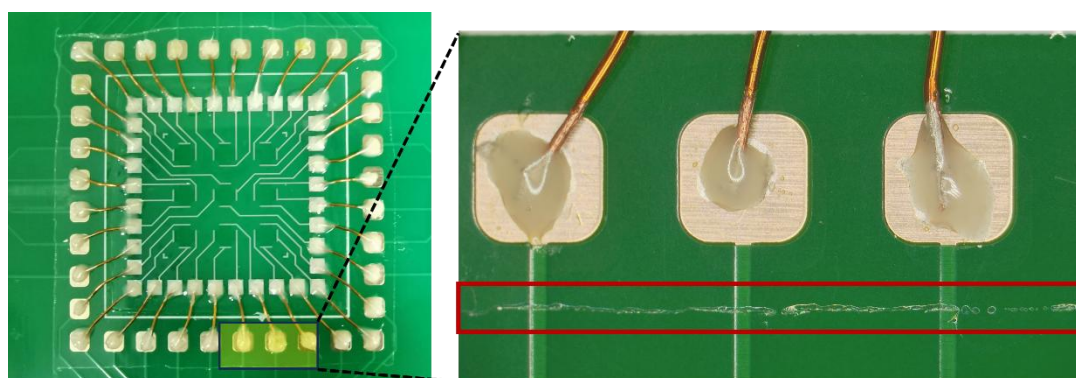
Supplementary Figure 1. Process Flow of graphene-based hall sensor.



Supplementary Figure 2. (A) SEM image of the graphene-based Hall sensor; (B) Raman characterization results of graphene.



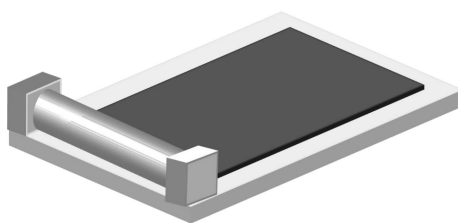
Supplementary Figure 3. EDS analysis results of the magnetic film: (A) SEM image; (B) EDS spectrum; (C and D) show the distribution of Fe, and Nd, respectively.



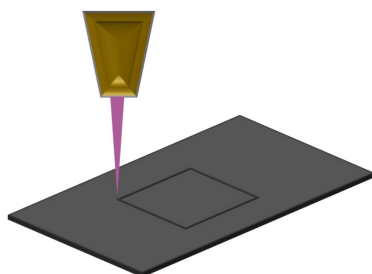
Supplementary Figure 4. Parylene-C deposition results.



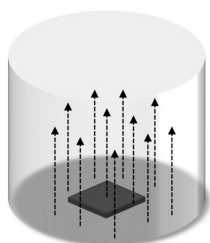
(A) Mix NdFeB powder and Dragon Skin 10 NV.



(B) Coating film.

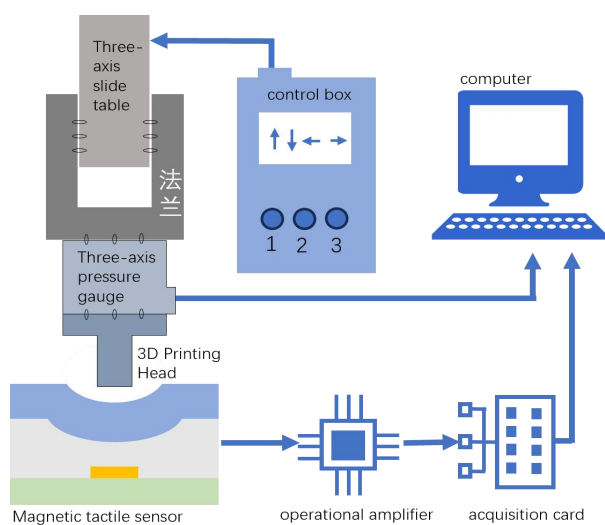


(C) Laser cutting.

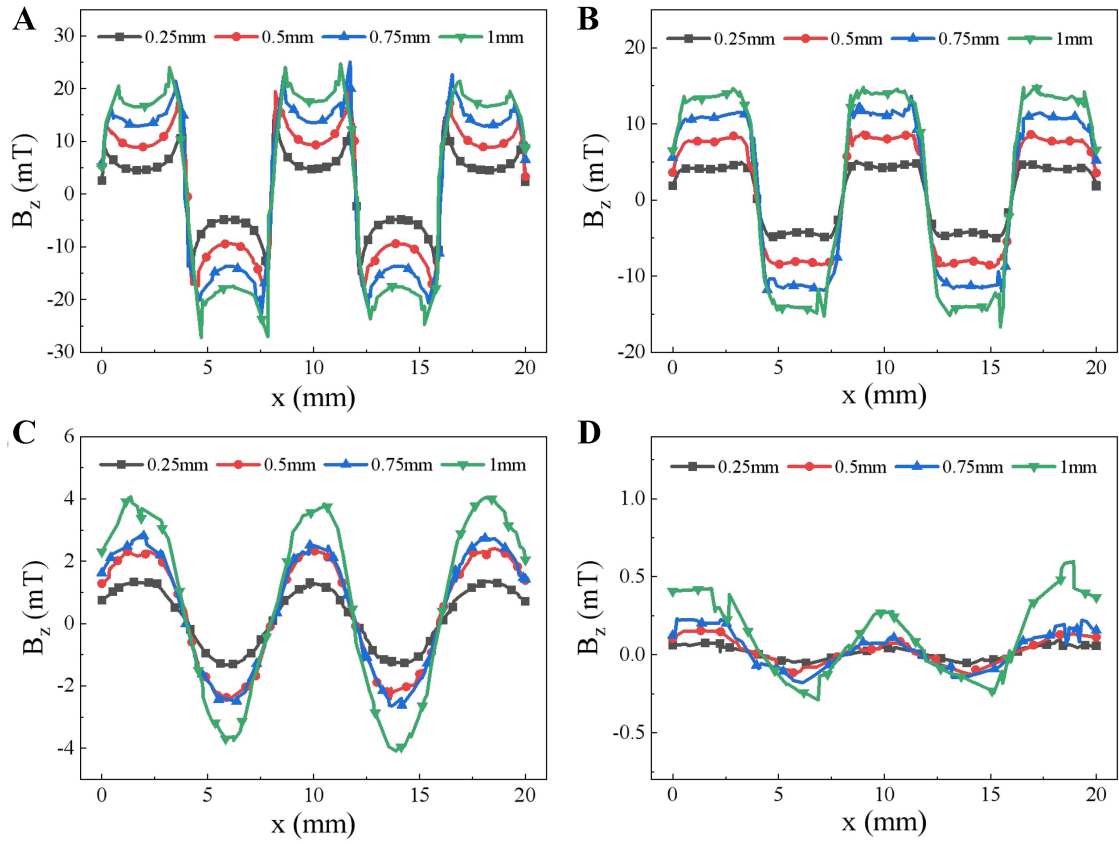


(D) Magnetization.

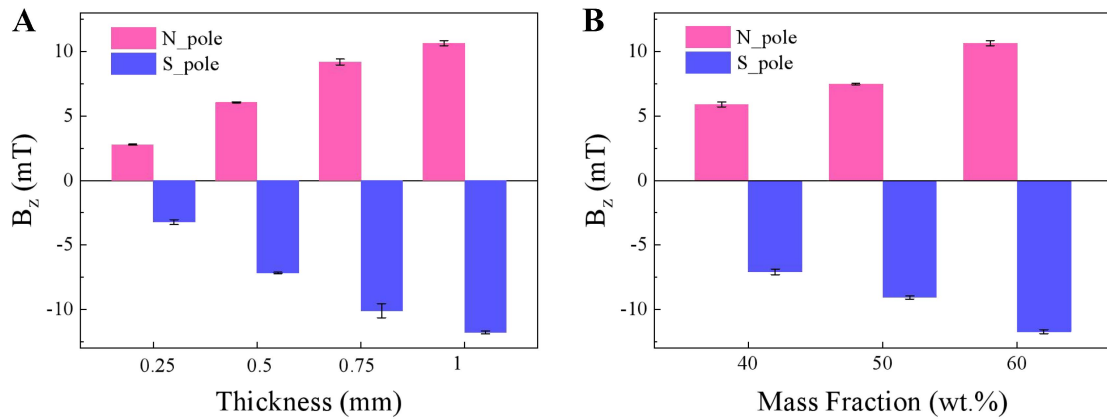
Supplementary Figure 5. Fabrication of magnetic films.



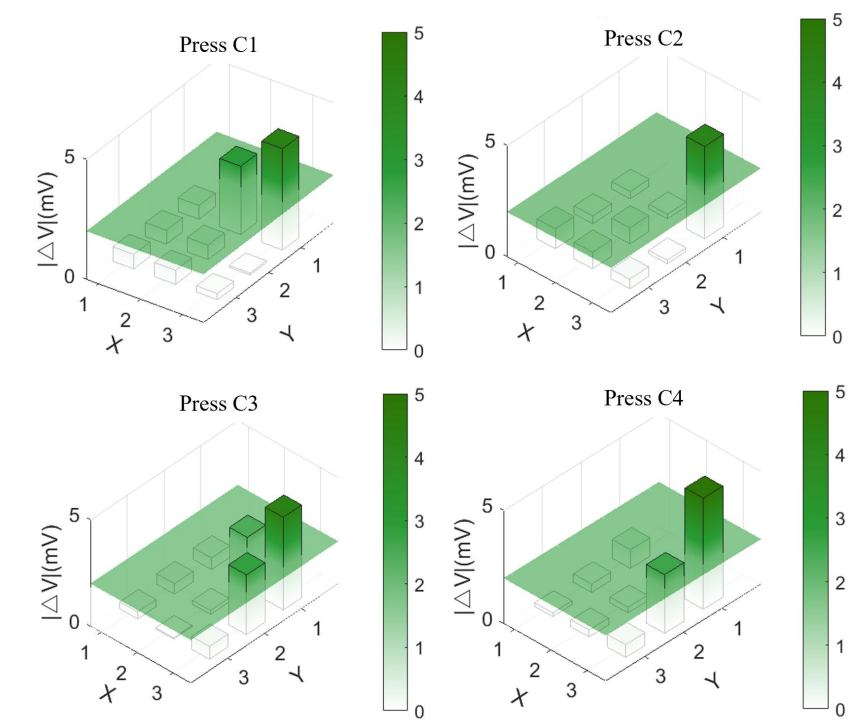
Supplementary Figure 6. Test system.



Supplementary Figure 7. Comparison of z-axis magnetic field simulations at different heights for different thicknesses of magnetic films. (A) $h_1 = 0.1$ mm. (B) $h_2 = 0.5$ mm. (C) $h_3 = 2$ mm. (D) $h_4 = 5$ mm.



Supplementary Figure 8. Test results of z-axis magnetic field for (A) different thicknesses and (B) different mass fractions of magnetic films.



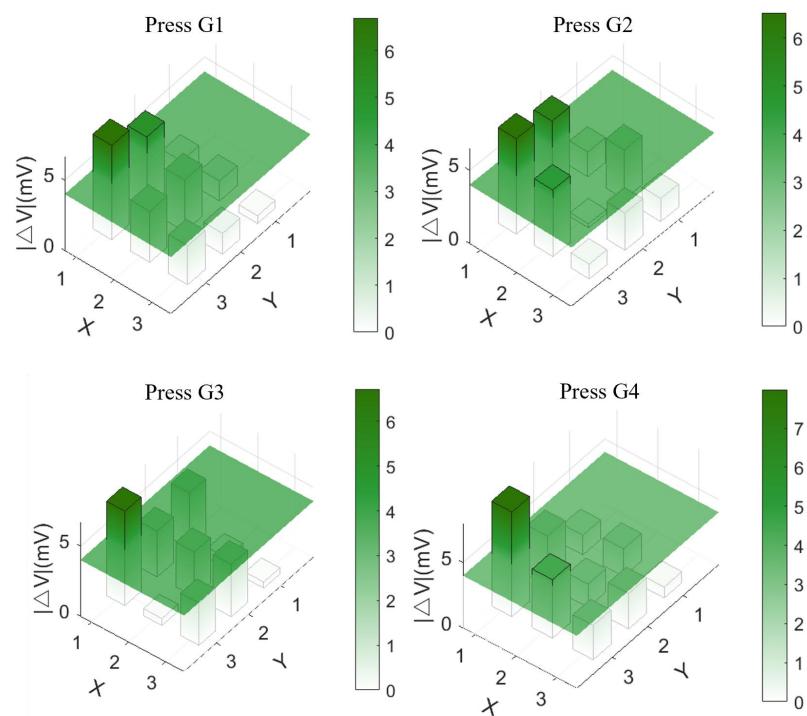
Supplementary Figure 9. Output comparison of pressing C1-C4.

Supplementary Table 1. Judgmental conditions for press C1-C4

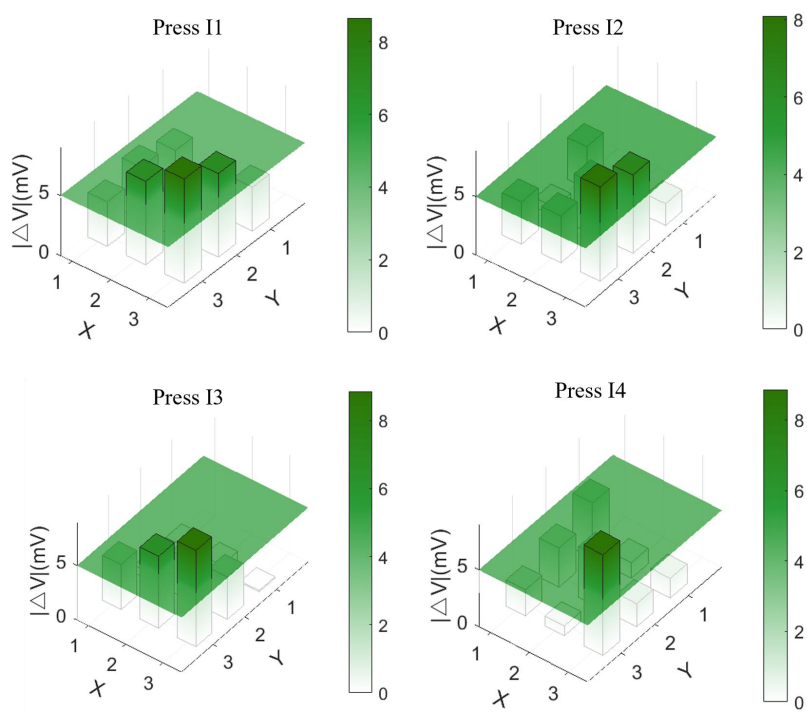
Condition	Result
$ \Delta V_{H3} > \Delta V_{Hi,i=1,2,4-9} $, $ \Delta V_{H2} > V_{h3}$, $ \Delta V_{Hj,j=1,4-9} < V_{h3}$	C1
$ \Delta V_{H3} > \Delta V_{Hi,i=1,2,4-9} $, $ \Delta V_{Hj,j=1,2,4-9} < V_{h3}$	C2
$ \Delta V_{H3} > \Delta V_{Hi,i=1,2,4-9} $, $ \Delta V_{H2} > V_{h3}$, $ \Delta V_{H6} > V_{h3}$, $ \Delta V_{Hj,j=1,4,5,7-9} < V_{h3}$	C3
$ \Delta V_{H3} > \Delta V_{Hi,i=1,2,4-9} $, $ \Delta V_{H6} > V_{h3}$, $ \Delta V_{Hj,j=1,2,4,5,7-9} < V_{h3}$	C4

Supplementary Table 2. Judgmental conditions for press C1-C4

Condition	Result
$ \Delta V_{H7} > \Delta V_{Hi,i=1-6,8-9} $, $ \Delta V_{H4} > V_{h7}$, $ \Delta V_{Hj,j=1-3,5,6,8,9} < V_{h7}$	G1
$ \Delta V_{H7} > \Delta V_{Hi,i=1-6,8-9} $, $ \Delta V_{H4} > V_{h7}$, $ \Delta V_{H8} > V_{h7}$, $ \Delta V_{Hj,j=1-3,5,6,9} < V_{h7}$	G2
$ \Delta V_{H7} > \Delta V_{Hi,i=1-6,8-9} $, $ \Delta V_{Hj,j=1-6,8-9} < V_{h7}$	G3
$ \Delta V_{H7} > \Delta V_{Hi,i=1-6,8-9} $, $ \Delta V_{H8} > V_{h7}$, $ \Delta V_{Hj,j=1-6,9} < V_{h7}$	G4



Supplementary Figure 10. Output comparison of pressing G1-G4.



Supplementary Figure 11. Output comparison of pressing I1-I4.

Supplementary Table 3. Judgmental conditions for press I1-I4

Condition	Result
$ \Delta V_{H9} > \Delta V_{Hi,i=1-8} , \Delta V_{H6} > V_{h9}, \Delta V_{H8} > V_{h9}, \Delta V_{Hj,j=1-5,7} < V_{h9}$	I1
$ \Delta V_{H9} > \Delta V_{Hi,i=1-8} , \Delta V_{H6} > V_{h9}, \Delta V_{Hj,j=1-5,7,8} < V_{h9}$	I2
$ \Delta V_{H9} > \Delta V_{Hi,i=1-8} , \Delta V_{H8} > V_{h9}, \Delta V_{Hj,j=1-7} < V_{h9}$	I3
$ \Delta V_{H9} > \Delta V_{Hi,i=1-8} , \Delta V_{Hj,j=1-8} < V_{h9}$	I4

Supplementary Table 4. Judgmental conditions for press D1-D4

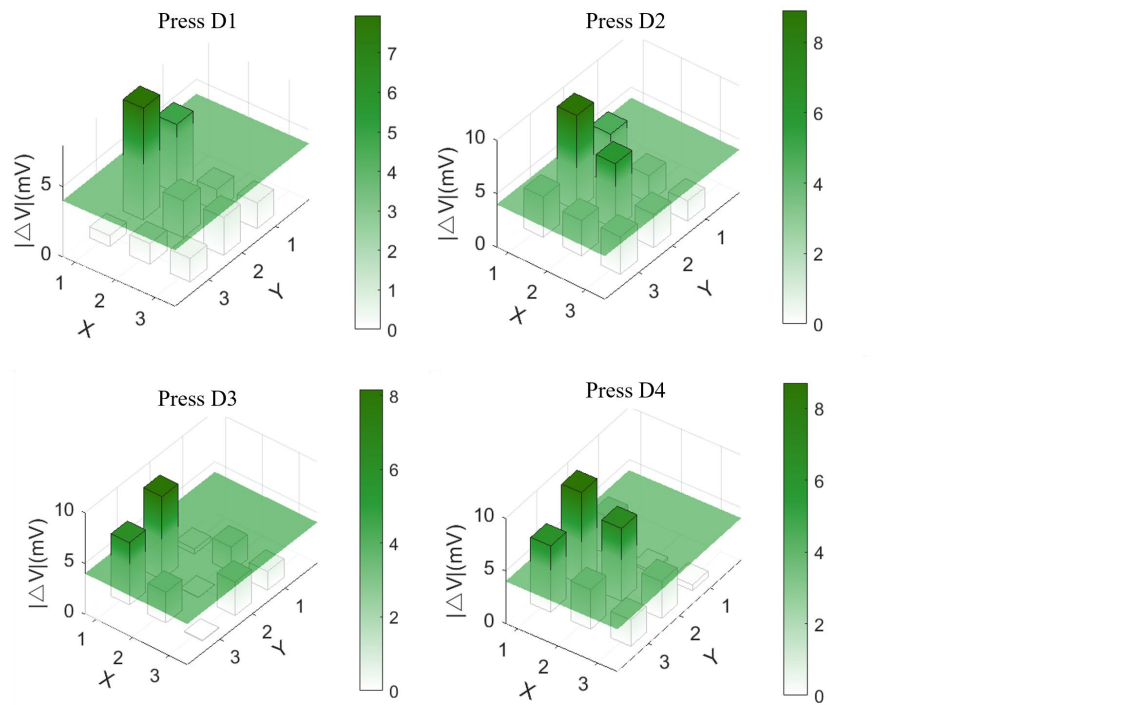
Condition	Result
$ \Delta V_{H4} > \Delta V_{Hi,i=1-3,5-9} , \Delta V_{H1} > V_{h4}, \Delta V_{Hj,j=2,3,5-9} < V_{h4}$	D1
$ \Delta V_{H4} > \Delta V_{Hi,i=1-3,5-9} , \Delta V_{H1} > V_{h4}, \Delta V_{H5} > V_{h4}, \Delta V_{Hj,j=2,3,6-9} < V_{h4}$	D2
$ \Delta V_{H4} > \Delta V_{Hi,i=1-3,5-9} , \Delta V_{H7} > V_{h4}, \Delta V_{Hj,j=1-3,5,6,8,9} < V_{h4}$	D3
$ \Delta V_{H4} > \Delta V_{Hi,i=1-3,5-9} , \Delta V_{H5} > V_{h4}, \Delta V_{H7} > V_{h4}, \Delta V_{Hj,j=1-3,6,8,9} < V_{h4}$	D4

Supplementary Table 5. Judgmental conditions for press F1-F4

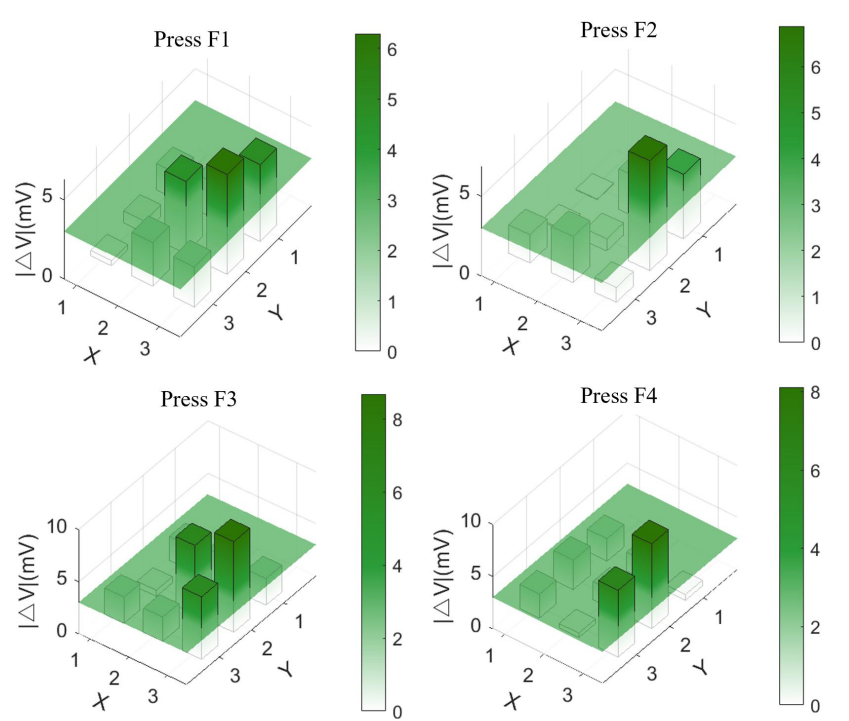
Condition	Result
$ \Delta V_{H6} > \Delta V_{Hi,i=1-5,7-9} , \Delta V_{H3} > V_{h6}, \Delta V_{H5} > V_{h6}, \Delta V_{Hj,j=1,2,4,7-9} < V_{h6}$	F1
$ \Delta V_{H6} > \Delta V_{Hi,i=1-5,7-9} , \Delta V_{H3} > V_{h6}, \Delta V_{Hj,j=1,2,4,5,7-9} < V_{h6}$	F2
$ \Delta V_{H6} > \Delta V_{Hi,i=1-5,7-9} , \Delta V_{H5} > V_{h6}, \Delta V_{H9} > V_{h6}, \Delta V_{Hj,j=1-4,7,8} < V_{h6}$	F3
$ \Delta V_{H6} > \Delta V_{Hi,i=1-5,7-9} , \Delta V_{H9} > V_{h6}, \Delta V_{Hj,j=1-5,7,8} < V_{h6}$	F4

Supplementary Table 6. Judgmental conditions for press H1-H4

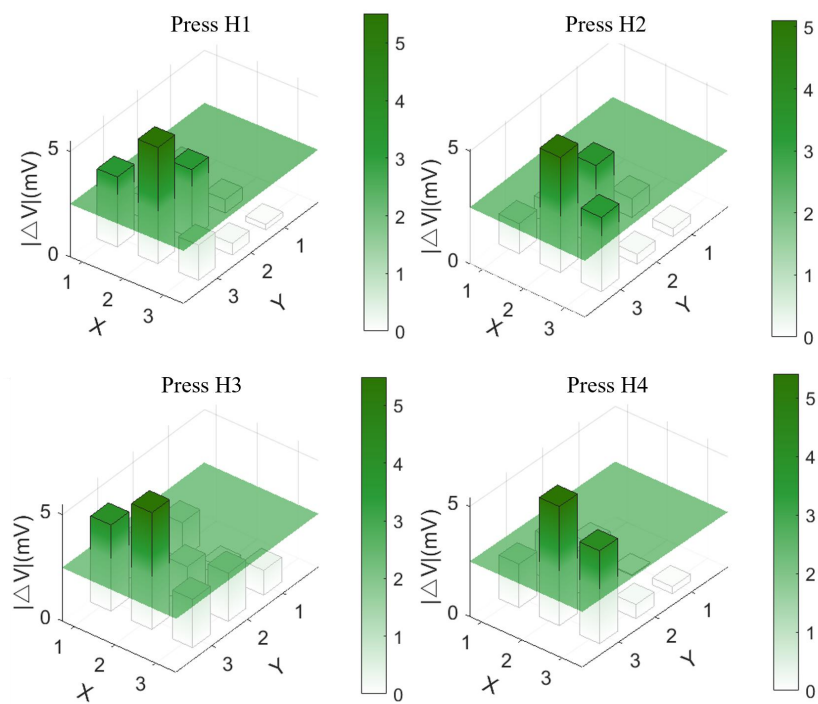
Condition	Result
$ \Delta V_{H8} > \Delta V_{Hi,i=1-7,9} , \Delta V_{H5} > V_{h8}, \Delta V_{H7} > V_{h8}, \Delta V_{Hj,j=1-4,6,9} < V_{h8}$	H1
$ \Delta V_{H8} > \Delta V_{Hi,i=1-7,9} , \Delta V_{H5} > V_{h8}, \Delta V_{H9} > V_{h8}, \Delta V_{Hj,j=1-4,6,7} < V_{h8}$	H2
$ \Delta V_{H8} > \Delta V_{Hi,i=1-7,9} , \Delta V_{H7} > V_{h8}, \Delta V_{Hj,j=1-6,9} < V_{h8}$	H3
$ \Delta V_{H8} > \Delta V_{Hi,i=1-7,9} , \Delta V_{H9} > V_{h8}, \Delta V_{Hj,j=1-7} < V_{h8}$	H4



Supplementary Figure 12. Output comparison of pressing D1-D4.



Supplementary Figure 13. Output comparison of pressing F1-F4.



Supplementary Figure 14. Output comparison of pressing H1-H4.

Supplementary Table 7. Performance comparison of sensors with similar functions

Ref.	Magnetization method	Linearity*	Hall Sensor Types	Resolution
[4]	sinusoidal magnetization	N/A	Commercial: MLX90393	3*3
[5]	Symmetrical up and down	0.95	Commercial: MLX90393	2*2
[6]	Opposite magnetization	0.97	Commercial: MLX90393	4*4
Our work	Periodic magnetization	0.97	Graphene Hall sensor	6*6

Supplementary Material Appendix A

The Hall sensor detects this variation in the magnetic field and outputs a corresponding Hall voltage.

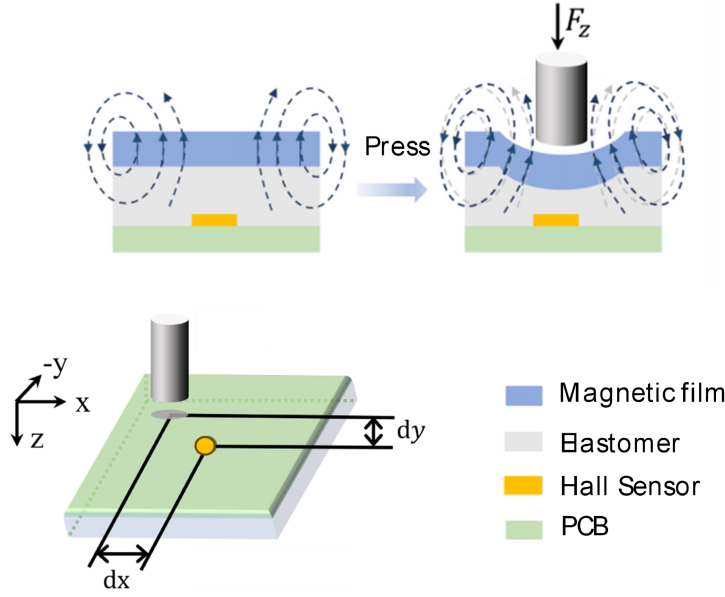


Figure A1-1. Schematic diagram of the magnetic tactile sensor.

For a magnetic film with a specific magnetization direction, when the film is not pressed, the initial magnetic field strength detected by the Hall sensor is:

$$B_{mag_initial} = \frac{B_{disc}}{r_{disc}^3} \quad (A-1)$$

Where, B_{disc} is the initial magnetic field at the pressed point, and r_{disc} is the distance between the Hall sensor and the pressed point. This distance can also be expressed as:

$$r_{disc} = \sqrt{dx^2 + dy^2 + z_{disc}^2} \quad (A-2)$$

Here, dx is the x-component of the horizontal distance between the Hall sensor and the pressed point, dy is the y-component of the horizontal distance, and z_{disc} is the initial vertical distance between the Hall sensor and the pressed point.

Substituting Equation (A-1) into Equation (A-2), we obtain:

$$B_{mag_initial} = \frac{B_{disc}}{(dx^2 + dy^2 + z_{disc}^2)^{1.5}} \quad (A-3)$$

When a certain pressure F is applied to the magnetic film at the pressed point, the vertical displacement of the point is Δz . This results in a change in the magnetic flux

density beneath the film. The variation in the magnetic field detected by the Hall sensor is expressed as:

$$\Delta B_{mag} \approx \left| \frac{\partial B_{mag}}{\partial z_{disc}} \right| \Delta z = \frac{3B_{disc}z_{disc}}{(dx^2+dy^2+z_{disc}^2)^{2.5}} \Delta z \quad (A-4)$$

For a given force F applied by the 3D-printed cylindrical indenter, the indentation depth on the elastomer surface can be estimated as:

$$\Delta z = \frac{F(1-\nu^2)}{2Er_a} \quad (A-5)$$

where ν is the Poisson's ratio of the material, E is the Young's modulus, and r_a is the radius of the cylindrical indenter. Substituting this expression into Equation (A-4), we obtain:

$$\Delta B_{mag} = \frac{3z_{disc}(1-\nu^2)}{2Er_a(dx^2+dy^2+z_{disc}^2)^{2.5}} B_{disc}F \quad (A-6)$$

It can be concluded that the magnetic field variation is approximately linearly proportional to the applied force. Defining the linear magnetoelastic coefficient as μ , we obtain $\Delta B_{mag} = \mu F$. Combining the Hall voltage formula, the relationship between the change in Hall voltage and the applied force can be derived as:

$$\Delta V_H = \frac{R_H}{H} I \Delta B_{mag} = \frac{R_H I}{H} \mu F \quad (A-7)$$

where H is the thickness of the Hall device, R_H is the Hall coefficient, and I is the magnitude of the current applied to the Hall element.